

Paper Set : SET-I(HT)

SUBJECT : Mathematics

ICSE Board - Sample Paper - 1 Solutions

SECTION - A

Q.1 (A) Let the speed of boat in still water = v

speed of stream = u

speed of boat in $v/s = v - u$

speed of boat in $d/s = v + u$

	d/s	u/s
D	30	30
s	$v + u$	$v - u$
t	$\frac{30}{v + u}$	$\frac{30}{v - u}$

D = Distance, S = Speed, t = Time.

$$\text{given } \frac{30}{v + u} + \frac{30}{v - u} = 4 \quad \frac{30}{60}$$

$$\frac{30}{15 + v} + \frac{30}{15 - v} = 4 \quad \frac{1}{2}$$

$$30 \left[\frac{1}{15 + u} + \frac{1}{15 - u} \right] = \frac{9}{2}$$

$$30 \left[\frac{30}{(15)^2 - v^2} \right] = \frac{9}{2}$$

$$200 = 225 - u^2.$$

$$u^2 = 25$$

$$u = 5 \text{ km/hr}$$

(B) $a_4 + a_8 = 24$

$$(a + 3d) + (a + 7d) = 24$$

$$2a + 10d = 24$$

$$a + 5d = 12$$

.... (i)

$$a_6 + a_{10} = 34$$

$$(a + 5d) + (a + 9d) = 34$$

$$2a + 14d = 34$$

$$a + 7d = 17 \quad \dots (ii)$$

From (i) and (ii)

$$a = -\frac{1}{2}$$

$$d = \frac{5}{2}$$

First 3 terms, $-\frac{1}{2}, 2, \frac{9}{2}$

(C) If 6 is the mean proportion of x and y

$$6 = \sqrt{xy}$$

$$36 = xy$$

$$36 \times 36 = x^2 y^2 \quad \dots (i)$$

48 is 3rd proportion to x and y

$$x : y = y : 48$$

$$\frac{x}{y} = \frac{y}{48}$$

$$y^2 = 48x \quad \dots (ii)$$

$$36 \times 36 = x^2 (48x) \quad [\text{From (i)}]$$

$$\frac{36 \times 36}{48} = x^3$$

$$x^3 = 27$$

$$x = 3 \text{ and } y = 12$$

Q.2 (A) Let the G.P. is

$$a, ar, ar^2, \dots, ar^{n-1}.$$

if each term raised to power x

$$a^x, (ar)^x, (ar^2)^x, \dots, (ar^{n-1})^x$$

$$a^x, a^x r^x, a^x r^{2x}, \dots, a^x r^{(n-1)x}$$

$$\frac{T_2}{T_1} = \frac{a^x r^x}{a^x} = r^x$$

$$\frac{T_3}{T_2} = \frac{a^x r^{2x}}{a^x r^x} = r^x$$

ratio of terms are same so it is a G.P. with common ratio r^x .

$$(B) \quad A \begin{bmatrix} 1 & 1 \\ -2 & 0 \end{bmatrix}, B \begin{bmatrix} 2 & -1 \\ 1 & 1 \end{bmatrix}$$

$$(i) \quad x + 2A = B$$

$$x = B - 2A$$

$$= \begin{bmatrix} 2 & -1 \\ 1 & 1 \end{bmatrix} - 2 \begin{bmatrix} 1 & 1 \\ -2 & 0 \end{bmatrix}$$

$$= \begin{bmatrix} 2 & -1 \\ 1 & 1 \end{bmatrix} - \begin{bmatrix} 2 & 2 \\ -4 & 0 \end{bmatrix}$$

$$\begin{bmatrix} 2-2 & -1-2 \\ 1-(-4) & 1-0 \end{bmatrix}$$

$$\begin{bmatrix} 0 & -3 \\ 5 & 1 \end{bmatrix}$$

$$(ii) \quad 3X + B + 2A = 0$$

$$3X = -B - 2A$$

$$X = \frac{1}{3} (-B - 2A)$$

$$X = \frac{1}{3} \left\{ - \begin{bmatrix} 2 & -1 \\ 1 & 1 \end{bmatrix} - 2 \begin{bmatrix} 1 & 1 \\ -2 & 0 \end{bmatrix} \right\}$$

$$= \frac{1}{3} \left\{ \begin{bmatrix} -2 & 1 \\ -1 & -1 \end{bmatrix} - \begin{bmatrix} 2 & 2 \\ -4 & 0 \end{bmatrix} \right\}$$

$$\frac{1}{3} \begin{bmatrix} -2-2 & 1-2 \\ -1+4 & -1-0 \end{bmatrix}$$

$$\frac{1}{3} \begin{bmatrix} -4 & -1 \\ 3 & -1 \end{bmatrix}$$

$$= \begin{bmatrix} -\frac{4}{3} & -\frac{1}{3} \\ 1 & -\frac{1}{3} \end{bmatrix}$$

$$(iii) \quad 3A - 2X = X - 2B$$

$$3A = 3X - 2B$$

$$3X = 3A + 2B$$

$$X \frac{1}{3}[3A \ 2B]$$

$$A \frac{2}{3}B$$

$$X \ A \ \frac{2}{3}B$$

$$\begin{bmatrix} 1 & 1 \\ -2 & 0 \end{bmatrix} \frac{2}{3} \begin{bmatrix} 2 & -1 \\ 1 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 1 \\ -2 & 0 \end{bmatrix} \begin{bmatrix} \frac{4}{3} & \frac{-2}{3} \\ \frac{2}{3} & \frac{2}{3} \end{bmatrix}$$

$$\begin{bmatrix} 1 + \frac{4}{3} & 1 - \frac{2}{3} \\ -2 & \frac{2}{3} \end{bmatrix} \begin{bmatrix} \frac{2}{3} \\ \frac{2}{3} \end{bmatrix}$$

$$\begin{bmatrix} \frac{7}{3} & \frac{1}{3} \\ -\frac{4}{3} & \frac{2}{3} \end{bmatrix}$$

Q.2 (C)

Output tax in Delhi (interstate) :

$$\text{IGST} = 9\% \text{ of } 50,000 = \text{Rs. } 9000$$

$$\text{Output tax in Delhi} = \text{Rs. } 9000$$

Output tax in Calcutta :

$$\text{C.P. in Calcutta} = \text{Rs. } 50,000 \text{ and Profit} = \text{Rs. } 20,000$$

$$\text{S.P. in Calcutta} = 50,000 + 20,000 = \text{Rs. } 70,000$$

$$\text{IGST} = 18\% \text{ of } 70,000 = \text{Rs. } 12,600$$

$$\text{Output tax in Calcutta} = \text{Rs. } 12,600$$

Since, the dealer in Nainital does not sell the product.

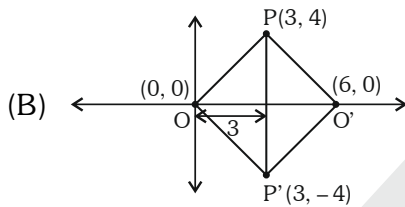
$$\text{Output GST (tax on sale)} = \text{Rs. } 0$$

Q.3 (A) Dividend = Divisor \times Quotient + remainder

$$3x^3 - 5x^2 + 6x + P = (x - 3)q(x) + 8$$

$$\begin{array}{r} x - 3 \overline{) 3x^3 - 5x^2 + 6x + P - 8} \\ \underline{3x^3 - 9x^2} \\ 4x^2 + 6x + P - 8 \\ \underline{4x^2 - 12x} \\ 18x + P - 8 \\ \underline{18x - 54} \\ P + 46 = 0 \quad P + 46 \end{array}$$

$$P = -46$$



(i) $P'(3, -4)$

$O'(6, 0)$

(ii) $PP' = 8$

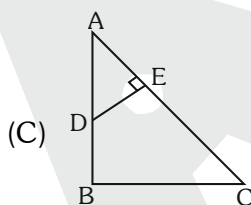
$OO' = 6$

(iii) Perimeter of quadrilateral $POP'O'$

$$= PO + OP' + P'O' + PO'$$

$$= 5 + 5 + 5 + 5 = 20$$

(iv) Rhombus



For $\triangle ADE \sim \triangle ACB$

$$\angle E = \angle B = 90^\circ$$

$\angle DAE = \angle BAC = \text{Common angle}$

So, $\triangle ADE \sim \triangle ACB$ [by AA similarity]

By CPST

$$\frac{AD}{AC} = \frac{DE}{CB} = \frac{AE}{AB}$$

$$\frac{AD}{13} = \frac{DE}{5} = \frac{4}{AB}$$

$$\frac{AD}{13} = \frac{DE}{5} = \frac{4}{12}$$

$$AD = \frac{13}{3}, DE = \frac{5}{3}$$

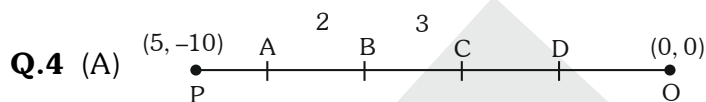
$$(iii) \text{Ar}(\triangle ADE) = \frac{1}{2} \times AE \times DE$$

$$= \frac{1}{2} \times 4 \times \frac{20}{8} = 5$$

$$\text{Ar}(\triangle ABC) = \frac{1}{2} \times 5 \times 8$$

$$= 20$$

$$\text{Ar}(\square BCED) = 20 - 5 = 15$$



B divide OP in 2 : 3 ratio

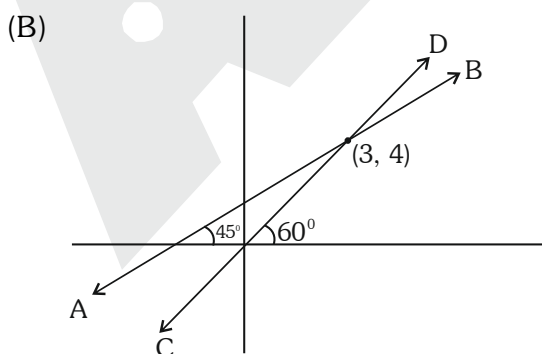
D divide OP in 4 : 1 ratio

$$B \left[\frac{2(0) + 3(5)}{2 + 3}, \frac{2(0) + 3(-10)}{2 + 3} \right]$$

$$B (3, -6)$$

$$D \left[\frac{4(0) + 1(5)}{4 + 1}, \frac{4(0) + 1(-10)}{4 + 1} \right]$$

$$D (1, -2)$$



Equation of line BC

$$y - y_1 = m (x - x_1)$$

$$y - 4 = \tan 60 (x - 3)$$

$$y - 4 = \sqrt{3}(x - 3)$$

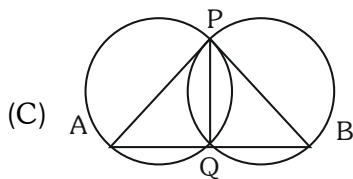
$$y - \sqrt{3}x - 4 + 3\sqrt{3} = 0$$

Equation of line AB

$$y - 4 = \tan 45 (x - 3)$$

$$y - 4 = x - 3$$

$$x - y + 1 = 0$$



$$\angle PQA = 90^\circ \quad \{\text{Diameter subtend } 90^\circ \text{ on circumference}\}$$

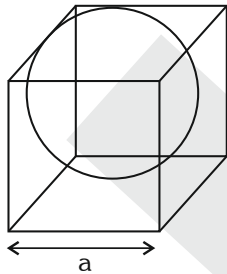
$$\angle BQP = 90^\circ$$

$$\angle PQA + \angle PQB = 180^\circ$$

So, A, Q, B are collinear.

Section B :

Q.5 (A)



$$a = 2r$$

$$V_c = a^3$$

$$V_s = \frac{4}{3}\pi r^3$$

$$= \frac{4}{3}\pi \left(\frac{a}{2}\right)^3$$

$$V_s = \frac{4}{3}\pi \left(\frac{a^3}{8}\right)$$

$$\frac{V_C}{V_S} = \frac{a^3}{\frac{4}{3}\pi\frac{a^3}{8}} = \frac{6}{\pi}$$

(B) $\frac{\sin A - \cos A}{\sin A + \cos A} \cdot \frac{1}{1 - \sin A} = \frac{\cos A}{1 - \sin A} \quad \{1 - \cos^2 A = \sin^2 A\}$

$$\text{L.H.S.} = \frac{\sin A - \cos A}{\sin A + \cos A} \cdot \frac{1}{1 - \sin A} \times \frac{\sin A}{\sin A} \cdot \frac{\cos A}{\cos A} \cdot \frac{1}{1}$$

$$\frac{(\sin A + 1)^2 - \cos^2 A}{(\sin A + \cos A)^2 - 1^2}$$

$$\Rightarrow \frac{\sin^2 A - \cos^2 A}{\sin^2 A + \cos^2 A - 1} = \frac{2 \sin A \cos A}{2 \sin A \cos A - 1}$$

$$\frac{2 \sin^2 A}{2 \sin A \cos A} = \frac{2 \sin A}{2 \sin A \cos A}$$

$$\frac{2 \sin A [1 - \sin A]}{2 \sin A \cos A}$$

$$= \frac{1 + \sin A}{\cos A} \times \frac{1 - \sin A}{1 - \sin A}$$

$$\frac{1 - \sin^2 A}{\cos A (1 - \sin A)} = \frac{\cos^2 A}{\cos A (1 - \sin A)}$$

$$\frac{\cos A}{1 - \sin A}$$

(C) 366 Days = 52 weeks + 2 Days.

2 days can be :

MON	TUE
TUE	WED
WED	TH
THE	FRI
FRI	SAT
SAT	SUN
SUN	MON

Favorable case = 2

Total case = 7

$$P = \frac{2}{7}$$

Q.6 (A)

Let Rs. X be invested in 9% Rs. 50 share at 8% premium and Rs. (20304 - X) be invested in 8% Rs. 25 share at 8% discount.

When Rs X is invested in 9% Rs. 50 share at 8% premium, we have Nominal value of share = Rs. 50

$$\text{Market value of share} = \text{Rs. } 50 + 8\% \text{ of Rs. } 50 = \text{Rs. } 50 \times \frac{108}{100} = \text{Rs. } 54$$

$$\text{Number of shares bought} = \frac{\text{Rs. } X}{\text{Rs. } 54} = \frac{X}{54}$$

$$\text{Dividend on each share} = 9\% \text{ of Rs. } 50 = \frac{9}{100} \times 50 = \text{Rs. } \frac{9}{2}$$

$$\text{Total dividend} = \text{Rs. } \frac{9}{2} \times \frac{X}{54} = \text{Rs. } \frac{X}{12}$$

When Rs. (20304 - X) is invested in 8% Rs. 25 Share at 8% discount, we have

Nominal value of share = Rs. 25

$$\text{Market value of share} = \text{Rs. } 25 - 8\% \text{ of Rs. } 25 = \text{Rs. } 25 \times \frac{92}{100} = \text{Rs. } 23$$

$$\text{Number of shares bought} = \frac{\text{Rs. } (20304 - x)}{\text{Rs. } 23} = \frac{20304 - x}{23}$$

$$\text{Dividend on each share} = 8\% \text{ of Rs. } 25 = \text{Rs. } \frac{8}{100} \times 25 = \text{Rs. } 2$$

$$\text{Total dividend} = \text{Rs. } 2 \times \frac{(20304 - x)}{23}$$

Given, dividends (or incomes) from both the investments are equal.

$$\therefore \frac{x}{12} = \frac{2(20304 - x)}{23}$$

$$\Rightarrow 23x = 24x - 24 \times 20304$$

$$\Rightarrow x = \frac{24 \times 20304}{47} = \text{Rs. } 10368$$

$$\therefore 20304 - x = 20304 - 10368 = 9936$$

Thus, Rs. 10368 is invested in 9% Rs. 50 share at 8% premium and Rs. 9936 is invested in 8% Rs. 25 share at 8% discount.

(B)

Weekly wages (Rs)	No. of Workers (f_i)	x_i	$f_i x_i$
50 – 55	5	52.5	262.5
55 – 60	20	57.5	1150
60 – 65	10	62.5	625
65 – 70	10	67.5	675
70 – 75	9	72.5	652.5
75 – 80	6	77.5	465
80 – 85	12	82.5	990
85 – 90	8	87.5	700
$\Sigma f_i = 80$		$\Sigma f_i x_i = 5520$	

(i) the mean $\bar{x} = \frac{\Sigma f_i x_i}{\Sigma f_i}$

$$\frac{5520}{80}$$

$$= 69$$

(ii) 55–60 is having maximum frequency so 55–60 is modal class.

(iii) No. of workers weekly wages < 80 is 60

No. of workers weekly wages greater than 65 and less than 80 are 25

(C) $\frac{Ar(\Delta_1)}{Ar(\Delta_2)} \left(\frac{P_1}{P_2} \right)^2 \left(\frac{A_1}{A_2} \right)^2 \left(\frac{M_1}{M_2} \right)^2 \quad \{\Delta_1 \sim \Delta_2\}$

P → Perimeter

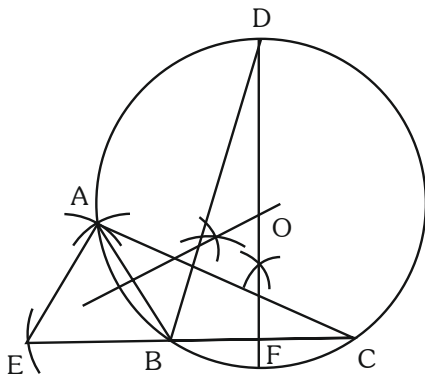
A → Length of latitude

M → Length of median

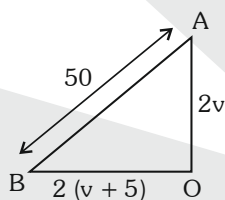
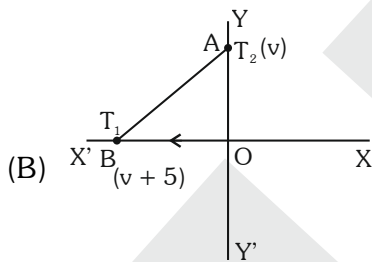
$$\frac{P_1}{P_2} \cdot \frac{A_1}{A_2} \cdot \frac{M_1}{M_2} \cdot \sqrt{\frac{Ar(\Delta_1)}{Ar(\Delta_2)}}$$

$$\frac{16}{25} \cdot \frac{4}{5}$$

Q.7 (A)



- Draw a line $BC = 5.4$ Cm.
- Draw $AB = 6$ cm, such that $m\angle ABC = 120^\circ$.
- Construct the perpendicular bisectors of AB and BC , such that they intersect at O .
- Draw a circle with center O and OA as the radius
- Extend the perpendicular bisector of BC , such that it intersects the circle at D .
- Here $BD = DC$.



$$AB^2 = OB^2 + OA^2$$

$$(50)^2 = [2(v + 5)]^2 + [2v]^2$$

$$2500 = 4[v^2 + 25 + 10v] + 4v^2$$

$$8v^2 + 40v - 2400 = 0$$

$$v^2 + 5v - 300 = 0$$

$$v^2 + 20v - 15v - 300 = 0$$

$$v(v + 20) - 15(v + 20) = 0$$

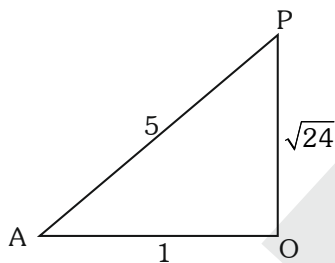
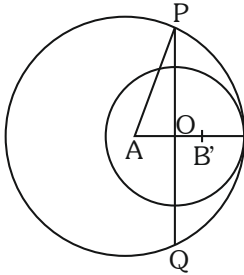
$$(v + 20)(v - 15) = 0$$

$$v = 15$$

Speed of train first = 15 km/hr

Speed of second train = 20 km/hr

Q.7 (C)



$$PQ = 2OP$$

$$2\sqrt{24}$$

$$4\sqrt{6}$$

Q.8 (A)
$$x = \frac{\sqrt{3a-2b}}{\sqrt{3a+2}-\sqrt{3a-2b}} \times \frac{\sqrt{3a-2b}}{\sqrt{3a-2b}} \times \frac{\sqrt{3a-2b}}{\sqrt{3a-2b}}$$

$$x = \frac{\sqrt{3a-2b} \cdot \sqrt{3a-2b}^2}{3a+2b - 3a-2b}$$

$$x = \frac{6a - 2\sqrt{3a-2b} \cdot 3a-2b}{4b}$$

$$x = \frac{3a + \sqrt{9a^2 - 4b^2}}{2b}$$

$$2bx - 3a = \sqrt{9a^2 - 4b^2}$$

$$(2bx - 3a)^2 = (9a^2 - 4b^2)$$

$$4b^2x^2 + 9a^2 - 12abx = 9a^2 - 4b^2$$

$$4b^2x^2 - 12abx + 4b^2 = 0$$

$$4b [bx^2 - 3ax + b] = 0$$

$$bx^2 - 3ax + b = 0$$

(B) Initial marked price by manufacturer A is Rs. 6000,

B bought the T.V. at discount of 20%.

Cost price of B = 80% of 6000 = Rs. 4800 (i)

GST paid by B for purchase = 18% of 4800 = Rs. 864 ... (ii)

B sells T.V. at discount of 10% of market Price.

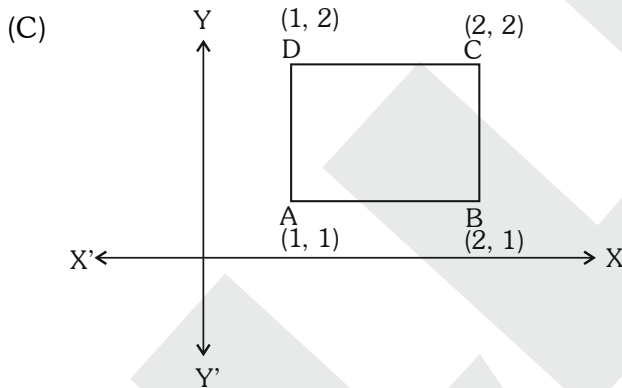
Selling price for B = 6000 - 10% of 600 = Rs. 5400(iii)

GST charged by B on selling of T.V. = 18% of 5400 = Rs. 972 (iv)

GST paid by B to the government = GST charged on selling price - GST paid against purchase price

$$= 972 - 864$$

$$= \text{Rs. } 108$$



Equation of line AB, $y = 1$

Equation of line BC, $x = 2$

Equation of line DC, $y = 2$

Equation of line AD, $x = 1$

Slope of diagonal AC

A(1, 1), C(2, 2)

$$\frac{1}{1} = 1$$

Slope of diagonal BD

B(2, 1), D(1, 2)

$$\frac{1}{-1} = -1$$

Q.9 (A)

Height(cm) (x_i)	No. of plants (f_i)	$f_i x_i$
50	2	100
55	4	220
58	10	580
60	f	60f
65	5	325
70	4	280
71	3	213
	Σf_i 28 f	$\Sigma f_i x_i$ 1718 60f

$$\bar{x} = \frac{\Sigma f_i x_i}{\Sigma f_i}$$

$$\frac{1718 + 60f}{28 + f} = 60.95$$

$$1718 + 60f = 1706.60 + 60.95f$$

$$11.4 = 0.95f$$

$$f = \frac{11.4}{0.95}$$

$$f = 12$$

(B) $3x + 5$ is a factor of polynomial

$$(a - 1)x^3 + (a + 1)x^2 - (2a + 1)x - 15 = 0$$

$$3x + 5 = 0$$

$$x = \frac{-5}{3} \text{ is zeroes of polynomial}$$

$$f(x) = (a - 1)x^3 + (a + 1)x^2 - (2a + 1)x - 15$$

$$= (a - 1)\left(\frac{-5}{3}\right)^3 + (a + 1)\left(\frac{-5}{3}\right)^2 - (2a + 1)\left(\frac{-5}{3}\right) - 15$$

$$f(x) = (a - 1)\left(\frac{-125}{27}\right) + (a + 1)\left(\frac{25}{9}\right) - (2a + 1)\left(\frac{5}{3}\right) - 15$$

$$0 = \frac{-125}{27}a + \frac{125}{27} + \frac{25a}{9} + \frac{25}{9} - \frac{10a}{3} - \frac{5}{3} - 15$$

$$\frac{125}{27}a - \frac{25a}{9} - \frac{10a}{3} + \frac{125}{27} + \frac{25}{9} - \frac{5}{3} - 15$$

$$= \frac{125a}{27} - \frac{25a}{9} - \frac{10a}{3} - \frac{125}{27} - \frac{25}{9} - \frac{5}{3} - \frac{15}{1}$$

$$\frac{125a - 75a - 90a}{27} - \frac{125}{27} - \frac{75}{9} - \frac{45}{3} - \frac{405}{27}$$

$$\frac{125a - 165a}{27} - \frac{245 - 405}{27}$$

$$-40a = -160$$

$$a = 4$$

The given polynomial is

$$3x^3 + 5x^2 - 9x - 15$$

(C),

1st Case

16% Rs. 100 shares at 80 means;

Market value of 1 share = Rs. 80

Nominal value of 1 share = Rs. 100

Dividend = 16%

Income on Rs. 80 = 16% of Rs. 100 = Rs. 16

Income on Rs. 1 = 16/80 of Rs. 0.20

2nd Case

20% Rs. 100 shares at 120 means;

Market value of 1 share = Rs. 120

Nominal value of 1 share = Rs. 100

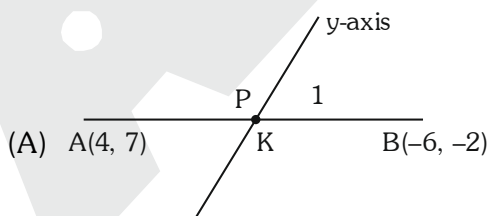
Dividend = 20%

Income on Rs. 120 = 20% of Rs. 100 = Rs. 20

Income on Rs. 1 = 20/120 = Rs. 0.17

Then 16% Rs. 100 shares at 80 is better investment.

Q.10



Let point K divide AB in P : 1 ratio

$$K \left[\frac{-6P + 4}{P + 1}, \frac{-2P + 7}{P + 1} \right]$$

Point K lies on y-axis, so x co-ordinate will be 0

$$\frac{-6P + 4}{P - 1} = 0$$

$$P = \frac{4}{6} = \frac{2}{3}$$

$$K \left[\frac{-6\left(\frac{2}{3}\right) + 4}{\frac{2}{3} - 1}, \frac{-2\left(\frac{2}{3}\right) + 7}{\frac{2}{3} - 1} \right]$$

$$K \left[0, \frac{17}{5} \right]$$

(B) (i) A perfect square number

1, 4, 9, 16, 25, 36, 49, 64, 81, 100

$$\text{Probability} = \frac{10}{100} = \frac{1}{10}$$

(ii) A number divisible by 4

4, 8, 12, 16, 20, 24, 28, 32, 36, 40, 44, 48, 52, 56, 60, 64, 68, 72, 76, 80, 84, 88, 92, 96, 100

$$\text{Probability} = \frac{25}{100} = \frac{1}{4}$$

(iii) A number divisible by 5

$$\text{Probability} = \frac{20}{100} = \frac{1}{5}$$

(iv) A number divisible by 4 or 5 number

$$\text{Probability} = \frac{25}{100} + \frac{20}{100} - \frac{5}{100} = \frac{40}{100}$$

(v) A number divisible by 4 and 5 both [20, 40, 60, 80, 100]

$$\frac{5}{100} = \frac{1}{20}$$

(C) Mean proportional of x and y

$$\sqrt{xy} = 14$$

$$xy = 196$$

$$x^2y^2 = 196 \times 196 \quad \dots(i)$$

For third proportion

$$x : y :: y : P$$

P is third proportion to x and y

$$\frac{x}{y} = \frac{y}{P}$$

$$y^2 = Px$$

$$y^2 = 112x \quad \dots(ii)$$

from (i) and (ii)

$$x^2(112x) = 196 \times 196$$

$$x^3 = \frac{196 \times 196}{112}$$

$$x^3 = 49 \times 7$$

$$x = 7$$

$$y = \frac{196}{7} = 28$$

Q.11

(A) $-2\frac{5}{6} < \frac{1}{2} - \frac{2x}{3} \leq 2, x \in \mathbb{W}$

$$-\frac{17}{6} < \frac{1}{2} - \frac{2x}{3} \leq 2, x \in \mathbb{W}$$

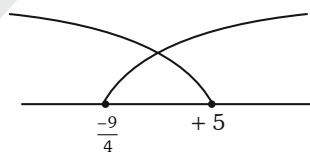
$$-\frac{17}{6} - \frac{1}{2} < -\frac{2x}{3} \leq 2 - \frac{1}{2}$$

$$\frac{-17-3}{6} < -\frac{2x}{3} \leq \frac{3}{2}$$

$$\frac{-20}{6} < -\frac{2x}{3} \leq \frac{3}{2}$$

$$\frac{20}{6} > \frac{2x}{3} \geq \frac{-3}{2}$$

$$5 > x \geq \frac{-9}{4}$$



(B) 120, 125, 130, 135,

Sum of all angles of polygon = $(n - 2)180$ (i)

120, 125, 130, 135,

120 + 125 + 130 + 135

$$\frac{n}{2}[2(120) + (n - 1)5] \dots (ii)$$

From (i) and (ii)

$$\frac{n}{2}[240 + (n - 1)5] = (n - 2) \times 180$$

$$120n + \frac{n}{2}(n - 1)5 = 180n - 360$$

$$120n + \frac{5}{2}n(n - 1) = 180n - 360$$

$$\frac{5}{2}(n^2 - n) = 60n - 360$$

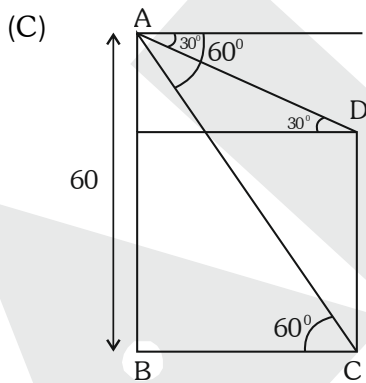
$$5n^2 - 5n = 120n - 720$$

$$5n^2 - 125n + 720 = 0$$

$$n^2 - 25n + 144 = 0$$

$$(n - 16)(n - 9) = 0, n = 16, n = 9$$

Ans. $n = 9$



(i) In ΔABC

$$\tan 60^\circ = \frac{AB}{BC}$$

$$\sqrt{3} = \frac{60}{BC}$$

$$BC = \frac{60}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}}$$

$$BC = 20\sqrt{3}$$

(ii) Height of lamp post

$$\tan 30 = \frac{AE}{ED}$$

$$\frac{1}{\sqrt{3}} = \frac{AE}{20\sqrt{3}}$$

$$AE = 20$$

$$CD = AB - AE$$

$$= 60 - 20 = 40 \text{ m}$$