

**JEE(Main) : Leader Course**
**ANSWER KEY**
**PART-1 : PHYSICS**

SECTION-I	Q.	1	2	3	4	5	6	7	8	9	10
	A.	B	B	A	C	C	D	B	D	B	B
SECTION-II	Q.	11	12	13	14	15	16	17	18	19	20
	A.	A	D	B	C	A	C	C	A	A	C

**PART-2 : CHEMISTRY**

SECTION-I	Q.	1	2	3	4	5	6	7	8	9	10
	A.	D	C	C	D	C	D	C	C	C	C
SECTION-II	Q.	11	12	13	14	15	16	17	18	19	20
	A.	A	A	C	B	A	B	C	C	C	B

**PART-3 : MATHEMATICS**

SECTION-I	Q.	1	2	3	4	5	6	7	8	9	10
	A.	B	C	A	C	C	C	D	C	A	A
SECTION-II	Q.	11	12	13	14	15	16	17	18	19	20
	A.	B	D	C	C	A	B	D	B	B	C

**HINT – SHEET**
**PART-1 : PHYSICS**
**SECTION-I**

 1. **Ans (B)**

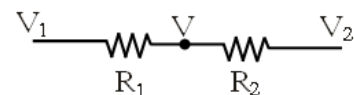
$$\vec{E} = (20x + 10)\hat{i}$$

$$V_1 - V_2 = \int_{-5}^1 (20x + 10) dx$$

$$V_1 - V_2 = -\left(10x^2 + 10x\right)_{-5}^1$$

$$V_1 - V_2 = 10(25 - 5 - 1 - 1)$$

$$V_1 - V_2 = 180 \text{ V}$$

 2. **Ans (B)**


$$V = \frac{V_1}{R_1} + \frac{V_2}{R_2}$$

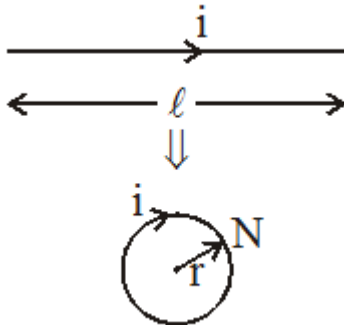
$$V = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2}}$$

4. **Ans (C)**

$$\ell = (2\pi r)N$$

$$M = Ni\pi r^2$$

$$= Ni\pi \left( \frac{\ell}{2\pi N} \right)^2$$



$$M \propto \frac{1}{N}$$

$$\frac{M_1}{M_2} = \frac{N_2}{N_1} = \frac{2}{1}$$

6. **Ans (D)**

$$\frac{1}{F} = \frac{1}{f_1} + \frac{1}{f_2} - \frac{d}{f_1 f_2}$$

$$0 = \frac{1}{20} + \frac{1}{f} - \frac{5}{20f}$$

$$0 = \frac{20 + f - 5}{20f}$$

$$f = -15 \text{ cm}$$

7. **Ans (B)**

Let  $v$  be the apparent depth of bubble then by

$$\text{using } \frac{\mu_2}{v} - \frac{\mu_1}{u} = \frac{\mu_2 - \mu_1}{R}$$

$$\therefore \frac{1}{v} - \frac{1.5}{-4} = \frac{1 - 1.5}{-10}$$

$$\Rightarrow v = -\frac{40}{13} = -3.07 \text{ cm}$$

8. **Ans (D)**

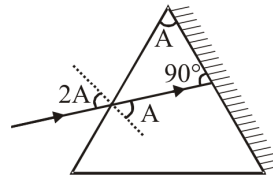
$$m_1 = - \left( \frac{f}{u_1 - f} \right)$$

$$m_2 = - \left( \frac{f}{u_2 - f} \right)$$

$$\frac{m_1}{m_2} = \frac{u_2 - f}{u_1 - f}$$

9. **Ans (B)**

$$\frac{\sin 2A}{\sin A} = \mu$$



$$\mu = 2\cos A$$

10. **Ans (B)**

$$\lambda = \frac{h}{\sqrt{2mk}}$$

11. **Ans (A)**

$$n_i^2 = n_e \times n_h$$

$$n_h = \frac{n_i^2}{n_e} = \frac{(1.41 \times 10^{16})^2}{10^{21}}$$

$$= 2 \times 10^{11} \text{ m}^{-3}$$

13. **Ans (B)**

$$\text{The de-Broglie wavelength } \lambda = \frac{h}{\sqrt{2mK}}$$

$$\text{Given } h = 6.6 \times 10^{-34} \text{ Js}$$

$$m = 1 \times 10^{-30} \text{ Kg}$$

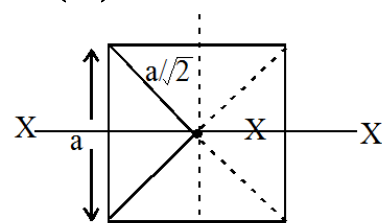
$$k = 200 \text{ eV} = 200 \times 1.6 \times 10^{-19} \text{ J}$$

Substituting all these values

$$\lambda = \frac{6.6 \times 10^{-34}}{\sqrt{2 \times 1 \times 10^{-30} \times 200 \times 1.6 \times 10^{-19}}}$$

$$= 0.825 \times 10^{-10} = 8.25 \times 10^{-11} \text{ m}$$

20. **Ans (C)**



X-X in axis of symmetry so centre of mass lie on X-X at centroid position of dotted triangle.

$$\frac{2}{3} \text{ (median of triangle)}$$

$$\frac{2}{3} \sqrt{\left( \frac{a}{\sqrt{2}} \right)^2 - \left( \frac{a}{2} \right)^2}$$

$$= \frac{2a}{3} \sqrt{\frac{1}{2} - \frac{1}{4}} = \frac{a}{6}$$



11. **Ans (A)**

Mass of solvent =  $a - c$

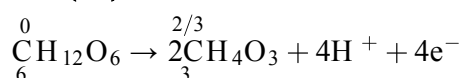
$$\text{Molality} = b = \left( \frac{c}{\text{mol.wt.}=?} \right) / \left( \frac{a-c}{1000} \right)$$

$$\therefore \text{mol. wt.} = \frac{1000 \times c}{b \times (a - c)}$$

12. **Ans (A)**

Larger the value of  $E^\circ_{\text{RP}}$  larger is tendency for reduction and consequently stronger will be the oxidant. Similarly, smaller the value of  $E^\circ_{\text{RP}}$  larger the tendency for oxidation and consequently stronger will be the reductant.

13. **Ans (C)**

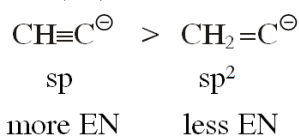


n-factor = 4

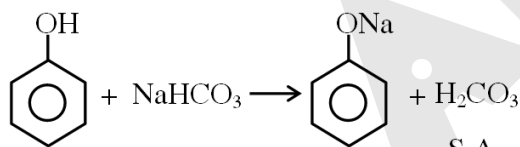
14. **Ans (B)**

Allene containing even no. of p-bond, shows optical isomerism if molecule is unsymmetrical.

16. **Ans (B)**



17. **Ans (C)**



W.A.

S.A.

Reaction always proceeds from S.A. to W.A., not from W.A. to S.A.

## PART-2 : CHEMISTRY

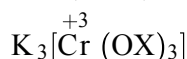
### SECTION-II

1. **Ans (4.00)**

Correct order are :

(i), (iii), (iv), (vi)

2. **Ans (3.00)**



(It has 3 unpaired electrons)

3. **Ans (4.00)**

$\text{S}_2, \text{N}_2, \text{RbO}_2$  and  $\text{ClO}_3$  are Paramagnetic

4. **Ans (4.04)**

$$\sqrt{3} a = 2 [r_{\text{Cs}^+} + r_{\text{Cl}^-}]$$

$$a = \frac{2[1.69 + 1.81]}{\sqrt{3}} = 4.04 \text{ \AA}$$

5. **Ans (112.00)**

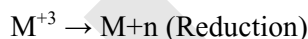
$$\text{mol of } \text{C}_2\text{H}_2 = \frac{1}{2} \times \text{mol of } \text{CHI}_3$$

$$= \frac{1}{2} \times 0.01 = 0.005$$

$$\text{vol. at N.T.P} = 0.005 \times 22400$$

$$= 112 \text{ ml}$$

6. **Ans (2.00)**



$$\text{n-factor} = (3 - n) \text{ e}^- \text{ gain}$$

(oxidation)

$$\text{n-factor} = (+4 \text{ to } +6)$$

$$= 2\text{e}^- \text{ loss}$$

$$\text{Total loss} = \text{Total gain}$$

$$0.1 \text{ M} \times (3 - n) \times 50 \text{ ml} = 0.1 \text{ M} \times (2) \times 25 \text{ ml}$$

$$3 - n = 1$$

$$n = 2$$

7. **Ans (2.00)**

$$p = \frac{n}{v} \cdot RT$$

$$\ell n p = \ell n \frac{n}{v} + \ell n RT$$

$$\log \frac{n}{v} = -0.3010$$

$$\log \frac{v}{n} = 0.3010$$

$$\frac{v}{n} = \text{anti log } 0.3010$$

$$\frac{v}{n} = 2$$

$$v = 2L$$

## PART-3 : MATHEMATICS

### SECTION-I

2. **Ans (C)**

$$(\text{AB})^2 = (\text{AB})(\text{AB}) = \text{A}(\text{BA})\text{B} = \text{A}^3\text{B}^2$$

$$\text{Now, } (\text{AB})^3 = \text{ABABAB} = \text{A}^7\text{B}^3$$

$$\text{So, } (\text{AB})^n = (\text{A})^{2^n - 1} \cdot \text{B}^n$$

$$\text{So, } K = 2^{10} - 1 = 1023$$

3. **Ans (A)**

$$\begin{aligned} \therefore \sum a^2 + \sum ab \leq 0 &\Rightarrow (a+b)^2 + (b+c)^2 + (c+a)^2 \leq 0 \\ \Rightarrow a+b=0, b+c=0, c+a=0 \\ \Rightarrow a=b=c=0 \end{aligned}$$

$$\therefore \begin{vmatrix} 4 & 0 & 1 \\ 1 & 4 & 0 \\ 0 & 1 & 4 \end{vmatrix} = 65$$

4. **Ans (C)**

Required ways

$${}^9C_6 \times \frac{6}{3 \times 3} - {}^{3 \times 6}C_6 \times \frac{6}{3 \times 3} = 1620$$

5. **Ans (C)**

Exhaustive cases (परिपूर्ण स्थितियाँ) = 26, 34, 43, 62 = 4

Favourable cases (अनुकूल स्थितियाँ) = 34, 43 = 2

$$\therefore \text{Required Probability} = \frac{1}{2}$$

6. **Ans (C)**

$Z_1(0, 4), Z_2(0, -4), k = 10$

$$|z_1 - z_2| = 8$$

$$k > |z_1 - z_2|$$

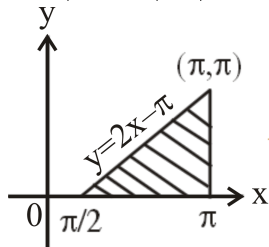
Ellipse

7. **Ans (D)**

$$y = \left| \frac{\pi}{2} - \sin^{-1}(\sin x) \right| + \left| \frac{\pi}{2} - \cos^{-1}(\cos x) \right|$$

$$y = \left| \frac{\pi}{2} - (\pi - x) \right| + \left| \frac{\pi}{2} - x \right|$$

$$y = \left| x - \frac{\pi}{2} \right| + \left| \frac{\pi}{2} - x \right| = 2x - \pi \quad \forall x \in \left[ \frac{\pi}{2}, \pi \right]$$



$$\text{Area} = \frac{1}{2} \left( \frac{\pi}{2} \right) \pi = \frac{\pi^2}{4}$$

8. **Ans (C)**

$$\begin{aligned} A &= \int_0^{\pi} \frac{\sin x}{x^2} dx \\ &= \left( \sin x \left( -\frac{1}{x} \right) \right)_0^{\pi} + \int_0^{\pi} \frac{\cos x}{x} dx \\ A &= 0 - (-1) + \int_0^{\pi} \frac{\cos x}{x} dx \end{aligned}$$

Put  $x = 2y$

$$A = 1 + \int_0^{\pi/2} \frac{\cos 2y}{y} dy$$

$$A = 1 + \int_0^{\pi/2} \frac{\cos 2x}{x} dx \quad [\text{By P-(1)}]$$

$$\int_0^{\pi/2} \frac{\cos 2x}{x} dx = A - 1$$

9. **Ans (A)**

Let  $y + 1 = Y$

$$\therefore \frac{dY}{dx} = Y^2 e^{\frac{x^2}{2}} - xY$$

$$\text{Put } -\frac{1}{Y} = k$$

$$\Rightarrow \frac{dk}{dx} + k(-x) = e^{\frac{x^2}{2}}$$

$$\text{I. F.} = e^{-\frac{x^2}{2}}$$

$$\therefore k = (x+c)e^{x^2/2}$$

$$\text{Put } k = -\frac{1}{y+1}$$

$$\therefore y+1 = -\frac{1}{(x+c)e^{x^2/2}} \quad \dots(i)$$

when  $x = 2, y = 0$ , then  $c = -2 - \frac{1}{e^2}$

differentiate equation (i) & put  $x = 1$

$$\text{we get } \left( \frac{dy}{dx} \right)_{x=1} = -\frac{e^{3/2}}{(1+e^2)^2}$$

14. Ans (C)

$$\bar{x} = \frac{\sum x_i}{n}$$

$$\Rightarrow 4 = \frac{1 + 2 + 6 + x_1 + x_2}{5}$$

$$\Rightarrow x_1 + x_2 = 11 \quad \dots(1)$$

$$\Rightarrow \sigma^2 = \frac{1}{n} \sum x_i^2 - \bar{x}^2$$

$$\Rightarrow 5.2 = \frac{1 + 4 + 36 + x_1^2 + x_2^2}{5} - 16$$

$$\Rightarrow 106 = x_1^2 + x_2^2 + 41$$

$$\Rightarrow x_1^2 + x_2^2 = 65 \quad \dots(2)$$

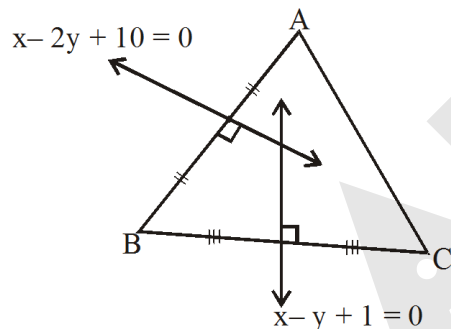
Solving (1) and (2)

$$x_1 = 4 \quad ; \quad x_2 = 7$$

15. Ans (A)

$p \rightarrow q$  will be false  
is  $P : T, q : F$   
 $(p \wedge \sim q) \wedge r \rightarrow \sim r : F$   
 $\Rightarrow \sim r = F$   
 $r = T$

16. Ans (B)



Circumcenter is the point of intersection of the perpendicular bisectors of the sides.

17. Ans (D)

Area of parallelogram formed by line  $y = m_1x + c_1$ ,  $y = m_1x + c_2$ ,  $y = m_2x + d_1$ ,  $y = m_2x + d_2$  is given by

$$\text{Area of parallelogram} = \left| \frac{(c_1 - c_2) \cdot (d_1 - d_2)}{m_1 - m_2} \right|$$

For the given lines

$$y = -\frac{x}{2} + \frac{5}{2}; y = -\frac{x}{2} + \frac{15}{2} \text{ and}$$

$$y = -3x + 10; y = -3x + \frac{c}{2},$$

$$\text{Area of parallelogram} = \frac{5 \cdot \left| \frac{c}{2} - 10 \right|}{\frac{5}{2}} \geq 1$$

(Given)

$$\Rightarrow |c - 20| \geq 1 \Rightarrow c \geq 21 \text{ or } c \leq 19$$

18. Ans (B)

Any point on the given hyperbola is

$$P(\sqrt{2} \sec \theta, \tan \theta)$$

Asymptotes are  $x - \sqrt{2}y = 0$ ,  $x + \sqrt{2}y = 0$

Product of perpendiculars from P on these asymptotes

$$= \frac{(\sqrt{2} \sec \theta - \sqrt{2} \tan \theta)(\sqrt{2} \sec \theta + \sqrt{2} \tan \theta)}{1 + 2}$$

$$= \frac{2 \sec^2 \theta - 2 \tan^2 \theta}{3} = \frac{2}{3}$$

19. Ans (B)

$$\text{Let } \vec{a} = \lambda \vec{b} + \mu \vec{c}$$

$\vec{a}$  is equally inclined to  $\vec{b}$  and  $\vec{d}$ , where

$$\vec{d} = \hat{j} + 2\hat{k}$$

$$\Rightarrow \frac{\vec{a} \cdot \vec{b}}{|\vec{a}| |\vec{b}|} = \frac{\vec{a} \cdot \vec{d}}{|\vec{a}| |\vec{d}|}$$

$$\Rightarrow \frac{(\lambda \vec{b} + \mu \vec{c}) \cdot \vec{b}}{\sqrt{5}} = \frac{(\lambda \vec{b} + \mu \vec{c}) \cdot \vec{d}}{\sqrt{5}}$$

$$\left[ \lambda (2\hat{i} + \hat{j}) + \mu (\hat{i} - \hat{j} + \hat{k}) \right] \cdot (2\hat{i} + \hat{j})$$

$$= \frac{\left[ \lambda (2\hat{i} + \hat{j}) + \mu (\hat{i} - \hat{j} + \hat{k}) \right] \cdot (\hat{j} + 2\hat{k})}{\sqrt{5}}$$

$$\text{or } \lambda(4 + 1) + \mu(2 - 1) = \lambda(1) + \mu(-1 + 2)$$

$$\text{or } 4\lambda = 0, \text{ i.e., } \lambda = 0$$

$$\therefore \hat{a} = \frac{\hat{i} - \hat{j} + \hat{k}}{\sqrt{3}}$$

20. **Ans ( C )**

According to  $\frac{A}{l} = \frac{B}{m} = \frac{C}{n}$ , direction ratio of plane are respectively (3,0,4).

Equation of plane passing through point (1, 1,1) is

$$\Rightarrow A(x - x_1) + B(y - y_1) + C(z - z_1) = 0$$

$$\Rightarrow 3(x - 1) + 0(y - 1) + 4(z - 1) = 0$$

$$\Rightarrow 3x + 4z - 7 = 0$$

Normal form of plane is,  $\frac{3x}{5} + \frac{4z}{5} = \frac{7}{5}$

$\therefore$  Perpendicular distance from (0,0,0) =  $\frac{7}{5}$ .

**PART-3 : MATHEMATICS**

**SECTION-II**

1. **Ans ( 1.00 )**

$$\frac{2^3 - 1^3}{1^3 \cdot 2^3} + \frac{3^3 - 2^3}{2^3 \cdot 3^3} + \frac{4^3 - 3^3}{3^3 \cdot 4^3} + \dots \infty$$

$$\left(\frac{1}{1^3} - \frac{1}{2^3}\right) + \left(\frac{1}{2^3} - \frac{1}{3^3}\right) + \left(\frac{1}{3^3} - \frac{1}{4^3}\right) + \dots \infty$$

$$\Rightarrow \lim_{n \rightarrow \infty} \left(\frac{1}{1^3} - \frac{1}{n^3}\right) = 1$$

2. **Ans ( 49.00 )**

Let  $T_{1+1}$  is max.

$$T_{1+1} = \frac{{}^{100}C_r}{(r+1)(r+2)(r+3)(r+4)}$$

$$= \frac{{}^{104}C_{r+4}}{101 \cdot 102 \cdot 103 \cdot 104} \text{ is max, when}$$

$$r+4 = 52$$

$$r = 48$$

so term is 49<sup>th</sup>

3. **Ans ( 11.00 )**

$$A_{10} + A_{12} = \int \tan^{10} x dx + \int \tan^{12} x dx$$

$$= \int (\tan^{10} x + \tan^{12} x) dx$$

$$= \int \tan^{10} x (1 + \tan^2 x) dx$$

$$= \int \tan^{10} x \cdot \sec^2 x dx$$

Let  $\int \tan x = t \Rightarrow \sec^2 x dx = dt$

$$A_{10} + A_{12} = \int t^{10} dt = \frac{t^{11}}{11} + \lambda$$

$$= \frac{\tan^{11} x + \lambda}{11}$$

4. **Ans ( 5.00 )**

$$I = \int (\sin 100x \cdot \cos x + \cos 100x \cdot \sin x) \sin^{99} x \cdot dx$$

$$I = \int \sin 100x \cdot \cos x \cdot \sin^{99} x dx + \int \cos 100x \sin^{100} x dx$$

$$I = \int \frac{\sin(100x) \sin^{100} x}{100} - \frac{100}{100} \int \cos(100x) \sin^{100} x dx +$$

$$\int \cos(100x) \cdot \sin^{100} x \cdot dx$$

$$I = \frac{\sin(100x) \sin^{100} x}{100} + C$$

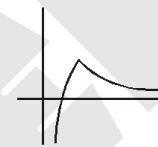
5. **Ans ( 3.00 )**

Do your self

6. **Ans ( 1.00 )**



Only one point of intersection



Sharp corner at one point

7. **Ans ( 4.00 )**

$$\tan^2 x - \sec^6 x + 1 = 0 \Rightarrow \sec^2 x = \sec^6 x$$

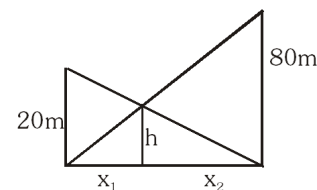
$$\sec^2 x \leq \sec^6 x \text{ as } |\sec x| > 1.$$

Hence only possible solutions are  $\sec^2 x = 1$

i.e.,  $x = n\pi$  as  $0 < x < 13$ ,

possible solutions are  $\pi, 2\pi, 3\pi, 4\pi$

8. **Ans ( 16.00 )**



by similar triangle

$$\frac{h}{x_1} = \frac{80}{x_1 + x_2} \dots(1)$$

$$\frac{h}{x_2} = \frac{20}{x_1 + x_2} \dots(2)$$

by (1) and (2)

$$\frac{x_2}{x_1} = 4 \text{ or } x^2 = 4x_1$$

$$\Rightarrow \frac{h}{x_1} = \frac{80}{5x_1}$$

or  $h = 16m$

9. Ans ( 20.00 )

Since, the given line touches the given circle, the length of the perpendicular from the centre (2, 4) of the circle to the line  $3x - 4y - k = 0$  is equal to the radius  $\sqrt{4 + 16 + 5} = 5$  of the circle.

$$\therefore \frac{3 \times 2 - 4 \times 4 - k}{\sqrt{9 + 16}} = \pm 5$$

$$\Rightarrow k = 15$$

[ $\because k > 0$ ]

hence equation of tangent is

$$3x - 4y - 15 = 0 \quad \dots (1)$$

Let equation of normal to circle

$$4x + 3y = \lambda$$

It passes through centre (2, 4)

$$\Rightarrow \lambda = 20$$

hence equation of normal is

$$4x + 3y = 20 \quad \dots (2)$$

Solve (1) & (2)

$$a = 5,$$

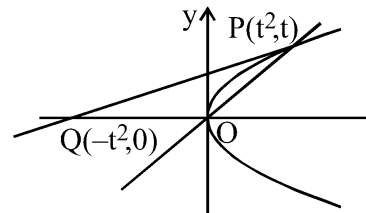
$$b = 0$$

$$k + a + b$$

$$= 15 + 5 + 0 = 20$$

10. Ans ( 0.50 )

$$\Delta OPQ = 4$$



$$\frac{1}{2} \begin{vmatrix} 0 & 0 & 1 \\ t^2 & t & 1 \\ -t^2 & 0 & 1 \end{vmatrix} = 4$$

$$t = 2 \quad (\because t > 0)$$

$$\therefore m = \frac{1}{2} = 0.50$$