

Q.No	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Ans	4	1	1	2	1	2	3	3	2	2	3	2	2	4	2
Q.No	16	17	18	19	20	21	22	23	24	25					
Ans	4	4	1	1	1	3	1	2	1	3					
Q.NO	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40
Ans	4	4	4	3	2	1	4	2	3	3	3	2	2	2	4
Q.NO	41	42	43	44	45	46	47	48	49	50					
Ans	4	4	4	4	1	3	2	2	4	2					
Q.NO	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65
Ans	1	1	2	2	1	1	4	3	3	1	1	4	1	4	3
Q.NO	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80
Ans	3	3	3	4	2	1	3	3	1	1	3	1	4	1	2
Q.No	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95
Ans	2	4	3	2	2	3	2	2	1	2	3	2	1	2	1
Q.No	96	97	98	99	100	101	102	103	104	105	106	107	108	109	110
Ans	2	4	3	4	1	2	2	2	2	2	3	4	3	2	2
Q.No	111	112	113	114	115	116	117	118	119	120					
Ans	1	3	1	2	2	4	1	3	2	3					

Q.No	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Ans	4	1	1	2	1	2	3	3	2	2	3	2	2	4	2
Q.No	16	17	18	19	20	21	22	23	24	25					
Ans	4	4	1	1	1	3	1	2	1	3					
Q.NO	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40
Ans	4	4	4	3	2	1	4	2	3	3	3	2	2	2	4
Q.NO	41	42	43	44	45	46	47	48	49	50					
Ans	4	4	4	4	1	3	2	2	4	2					
Q.NO	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65
Ans	1	1	2	2	1	1	4	3	3	1	1	4	1	4	3
Q.NO	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80
Ans	3	3	3	4	2	1	3	3	1	1	3	1	4	1	2
Q.No	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95
Ans	2	4	3	2	2	3	2	2	1	2	3	2	1	2	1
Q.No	96	97	98	99	100	101	102	103	104	105	106	107	108	109	110
Ans	2	4	3	4	1	2	2	2	2	2	3	4	3	2	2
Q.No	111	112	113	114	115	116	117	118	119	120					
Ans	1	3	1	2	2	4	1	3	2	3					

Q.No	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Ans	4	1	1	2	1	2	3	3	2	2	3	2	2	4	2
Q.No	16	17	18	19	20	21	22	23	24	25					
Ans	4	4	1	1	1	3	1	2	1	3					
Q.NO	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40
Ans	4	4	4	3	2	1	4	2	3	3	3	2	2	2	4
Q.NO	41	42	43	44	45	46	47	48	49	50					
Ans	4	4	4	4	1	3	2	2	4	2					
Q.NO	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65
Ans	1	1	2	2	1	1	4	3	3	1	1	4	1	4	3
Q.NO	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80
Ans	3	3	3	4	2	1	3	3	1	1	3	1	4	1	2
Q.No	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95
Ans	2	4	3	2	2	3	2	2	1	2	3	2	1	2	1
Q.No	96	97	98	99	100	101	102	103	104	105	106	107	108	109	110
Ans	2	4	3	4	1	2	2	2	2	2	3	4	3	2	2
Q.No	111	112	113	114	115	116	117	118	119	120					
Ans	1	3	1	2	2	4	1	3	2	3					

MOCK TEST

PAPER CODE
B

EXAM DATE : 26.11.2017

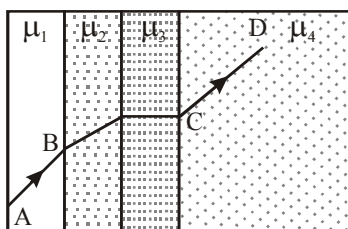
TIME
1.30 Hours (PCM)
1.30 Hours (PCB)

FORM NUMBER :

MAXIMUM MARKS
PCM - 80 MARKS
PCB - 90 MARKS

ANSWER KEY & SOLUTION

1. A ray of light passes through four transparent media with refractive indices μ_1, μ_2, μ_3 and μ_4 as shown in the figure, the surfaces of all media are parallel. If the emergent ray CD is parallel to the incident ray AB, we must have



- (1) $\mu_1 = \mu_2$ (2) $\mu_2 = \mu_3$
(3) $\mu_3 = \mu_4$ (4) $\mu_4 = \mu_1$

Ans. 4

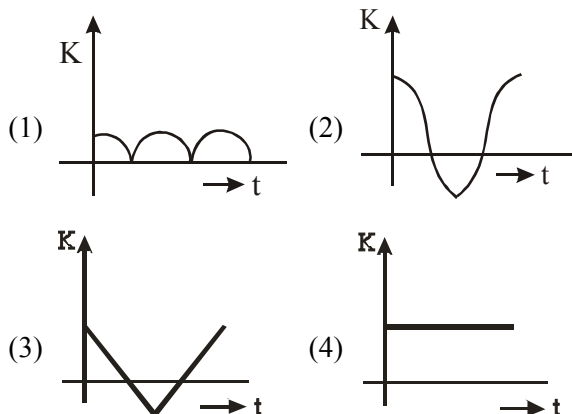
Sol. According to Snell's Law,

$$\mu \sin \theta = \text{constant}$$

which gives

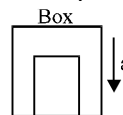
$$\mu_1 = \mu_4.$$

2. A body performs S.H.M. Its kinetic energy, K , varies with time t , as indicated in the graph :



Ans : 1

3. With what acceleration 'a' should the box in the figure descend so that a body of mass M placed in it exerts a force $\frac{Mg}{4}$ on the base of the box ?



- (1) $\frac{3g}{4}$ (2) $\frac{g}{4}$ (3) $\frac{g}{2}$ (4) $\frac{g}{8}$

Ans : 1

Sol. If the box is accelerated downwards, from the frame outside the elevator, equation of motion can be written as

$$Mg - N = Ma$$

$$\text{Here, } N = \frac{Mg}{4}$$

$$\Rightarrow a = \frac{3g}{4}$$

4. The magnetic flux through each turn of a 100 turn coil is $(t^3 - 2t) \times 10^{-3}$ Wb, where t is in second. The induced emf at $t = 2$ s is

- (1) -4V (2) -1V
(3) +1V (4) +4V

Ans. 2

$$\text{Sol. } \phi = (t^3 - 2t) \times 10^{-3}$$

$$\frac{d\phi}{dt} = (3t^2 - 2) \times 10^{-3}$$

$$\left. \frac{d\phi}{dt} \right|_{t=2} = (3 \times 4 - 2) \times 10^{-3} \text{ Wb/s}$$

$$= 10^{-2} \text{ Wb/s}$$

$$e = -N \frac{d\phi}{dt} = -100 \times 10^{-2} \text{ V} = -1 \text{ V.}$$

5. Resonance frequency of a circuit is f . If the capacitance is made 4 times the initial value, then the resonance frequency will become :

- (1) $f/2$ (2) $2f$
(3) f (4) $f/4$

Ans. 1

Sol. $f = \frac{1}{2\pi\sqrt{LC}}$ i.e. $f \propto \frac{1}{\sqrt{C}} \rightarrow \frac{1}{\sqrt{4}} = \frac{1}{2}$ time

6. A uniform wire has electric resistance R . The wire is cut into n equal parts. All wires are put parallel to each other and joined at the ends. The resistance of the combination is

- (1) R/n (2) R/n^2
(3) R (4) None of these.

Ans. 2

Sol. $\therefore R = \rho \frac{l}{A}$
 $\therefore R \propto l$

Hence, resistance of each wire is $\frac{R}{n}$

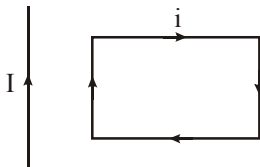
For the resistance of the combination,

$$\frac{1}{R'} = \frac{n}{R} + \frac{n}{R} + \frac{n}{R} + \dots \dots n \text{ times}$$

$$= \frac{n}{R} \times n$$

$$R' = \frac{R}{n^2}$$

7. A regular loop carrying a current i is situated near a long straight wire such that the wire is parallel to one of the sides of the loop and is in the plane of the loop. If a steady current I established in the wire as shown in the figure, the loop will :



- (1) Rotate about an axis parallel to the wire
(2) Move away from the wire
(3) Move towards the wire
(4) Remain stationary.

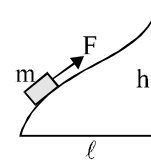
Ans. 3

Sol. $F = \frac{\mu_0 i I}{2\pi r}$

$F_{\text{attraction}} > F_{\text{repulsion}}$

Hence the loop will move towards the wire.

8. A body of mass m is slowly pulled up the hill by a force F which at each point was directed along the tangent of the trajectory as shown in figure. All surfaces are smooth. Find the work performed by this force



- (1) mg/l (2) $-mg/l$
(3) mgh (4) Zero

Ans : 3

Sol. $\sum W_{\text{net}} = \Delta K$

as particle is moving slowly, this means $\Delta K = 0$

$$\Rightarrow W_N + W_F + W_{mg} = \Delta K$$

but $W_N = 0$, as $\vec{N} \perp d\vec{r}$

$$\Rightarrow 0 + W_f - mgh = 0$$

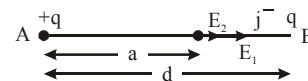
$$\Rightarrow W_f = mgh$$

9. There are points on a straight line joining two fixed opposite charges. There is :

- (1) No point where potential is zero
(2) Only one point where potential is zero
(3) No point where electric field is zero
(4) Only one point where electric field is zero.

Ans. 2

Sol. Let two opposite charges $+q$ and $-q$ be situated at points A and B respectively.



$$E_1 = \frac{1}{4\pi\epsilon_0} \frac{q}{a^2}$$

$$E_2 = \frac{1}{4\pi\epsilon_0} \frac{q}{(d-a)^2}$$

$$E = E_1 + E_2$$

$$= \frac{q}{4\pi\epsilon_0} \left[\frac{1}{a^2} + \frac{1}{(d-a)^2} \right]$$

$$= \frac{q}{4\pi\epsilon_0} \left[\frac{d^2 - 2ad + a^2 + a^2}{a^2(d-a)^2} \right]$$

Hence, there can be more than one point where electric field is zero.

$$V_1 = \frac{1}{4\pi\epsilon_0} \frac{q}{a}; V_2 = \frac{1}{4\pi\epsilon_0} \frac{(-q)}{(d-a)}$$

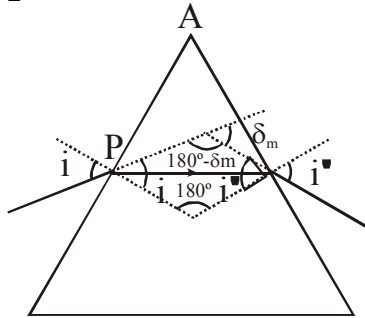
$$V = V_1 + V_2$$

10. A ray of light passes through an equilateral prism such that the angle of incidence and the angle of emergence are both equal to $\frac{3}{4}$ th of the angle of prism. The angle of minimum deviation is

- (1) 15° (2) 30°
(3) 45° (4) 60°

Ans. 2

Sol:



Given $A = 60^\circ$

$$i = i' = \frac{3}{4}A = 45^\circ \quad \therefore \quad i + i' = A + \delta$$

$$\text{or } 90^\circ = 60^\circ + \delta$$

$$\therefore \delta = 30^\circ$$

Note that $i = i'$ is the condition for minimum deviation.

Hence $\delta = 30^\circ = \delta_{\min}$

11. A body when projected vertically up, covers a total distance D , during the time of its flight t . If there were no gravity, the distance covered by it during the same time is equal to

- (1) 0 (2) D
(3) $2D$ (4) $4D$.

Ans : 3

Sol.

The displacement of the body during the time t as it attains the point of projection

$$\Rightarrow S = 0$$

$$\Rightarrow v_0 t - \frac{1}{2} g t^2 = 0$$

$$\Rightarrow t = \frac{2v_0}{g}$$

During the same time t , the body moves in absence of gravity through a distance

$$D' = v_0 t, \text{ because in absence of gravity } g = 0$$

$$\Rightarrow D' = v_0 \left(\frac{2v_0}{g} \right) = \frac{2v_0^2}{g} \quad \dots(i)$$

In presence of gravity the total distance covered is

$$= D = 2H = 2 \frac{v_0^2}{2g} = \frac{v_0^2}{g} \quad \dots(ii)$$

$$(i) \div (ii) \Rightarrow D' = 2D$$

12. A 6×10^{-9} F parallel plate capacitor is connected to a 500 V battery. When air is replaced by another dielectric material. 7.5×10^{-6} C charge flows into the capacitor. The dielectric constant of the material is:

- (1) 1.0 (2) 3.5
(3) 2.0 (4) 4.5

Ans. 2

Sol.

$$Q = CV$$

$$Q_1 = 6 \times 10^{-9} \times 500 \\ = 3 \times 10^{-6} \text{ C}$$

After insertion of dielectric

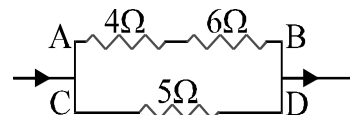
$$Q'_1 = (3+7.5) \times 10^{-6} \text{ C} \\ = 10.5 \times 10^{-6} \text{ C}$$

$$Q'_1 = CVK$$

$$10.5 \times 10^{-6} = 6 \times 10^{-9} \times 500 K$$

$$K = 3.5$$

13. In the circuit shown in figure the heat produced in the 5 ohm resistor due to the current flowing through it is 10 calories per second. The heat generated in the 4 ohms resistor is



- (1) 1 calorie/sec (2) 2 calories/sec
(3) 3 calories/sec (4) 4 calories/sec

Ans. 2

Sol. Let I_1 be the current flowing in 5Ω resistance and $(I - I_1)$ in 4Ω and 6Ω resistance.

The heat generated in 5Ω resistor is

$$10 \text{ cal/s} = 4.2 \times 10 \text{ J/s}$$

$$\therefore 4.2 \times 10 = I_1^2 R$$

$$\therefore I_1 = \sqrt{\frac{4.2 \times 10}{5}} = \sqrt{8.4} = 2.9 \text{ amp} \quad \dots(i)$$

Since AB and CD are in parallel.

\therefore The potential difference remains the same between C and D; and between A and B.

$\therefore (I - I_1)(4 + 6) = I_1 \times 5$ on solving using I_1 from (i) we get

$$(I - 2.9) 10 = 2.9 \times 5$$

$$\therefore I - 2.9 = 1.45$$

$$\therefore I = 4.35$$

Heat released/sec in 4 W resistance will be

$$= (4.35 - 2.9)^2 \times 4$$

$$= 8.4 \text{ J/s}$$

$$= 2 \text{ cal/s}$$

$$= \frac{q}{4\pi\epsilon_0} \left[\frac{1}{a} - \frac{1}{d-a} \right] = \frac{q(d-2a)}{4\pi\epsilon_0 a(d-a)}$$

\therefore Potential is zero only at $d = 2a$ or $a = d/2$

14. A certain charge Q is divided into two parts q and $(Q-q)$. For the maximum coulomb force between them, the ratio (q/Q) is :

(1) $1/16$

(2) $1/8$

(3) $1/4$

(4) $1/2$

Ans. 4

Sol. $F = \frac{1}{4\pi\epsilon_0} \frac{q(Q-q)}{r^2}$

for F to be maximum, $\frac{dF}{dq} = 0$

$$\frac{1}{4\pi\epsilon_0} \cdot \frac{1}{r^2} [Q - q + q(-1)] = 0$$

$$Q - 2q = 0$$

$$\frac{q}{Q} = \frac{1}{2}$$

15. A uniform electric field pointing in positive x -direction exists in a region. Let A be the origin, B be the point on the x -axis at $x = +1$ cm and C be point on the y -axis at $y = +1$ cm. Then the potentials at the points A , B and C satisfy :

(1) $V_A < V_B$

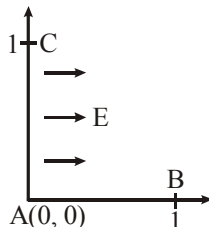
(2) $V_A > V_B$

(3) $V_A < V_C$

(4) $V_A > V_C$

Ans. 2

Sol.



Direction of electric field is in the direction of potential drop

$$\Rightarrow V_A > V_B$$

$$V_A = V_C$$

16. An ammeter and a voltmeter are joined in series to a cell. Their readings are A and V respectively. If a resistance is now joined in parallel with the voltmeter.

(1) Both A and V will increase

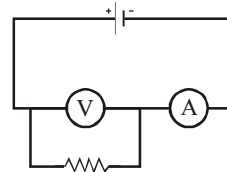
(2) Both A and V will decrease

(3) A will decrease, V will increase

(4) A will increase, V will decrease.

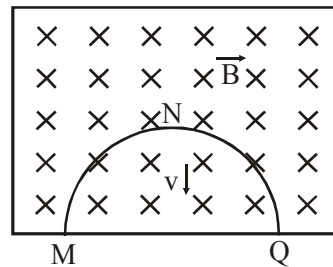
Ans. 4

Sol.



When a resistance is joined in parallel with the voltmeter, the total resistance of the circuit decreases. Current will increase and ammeter reading will increase. Potential difference across the ammeter increases thus potential difference across voltmeter decreases.

17. A thin semi-circular conducting ring of radius R is falling with its plane vertical in a horizontal magnetic induction \vec{B} (see figure). At the position MNQ the speed of the ring is v and the potential difference developed across the ring is



(1) zero

(2) $Bv\pi R^2/2$

(3) πRBv

(4) $2RBv$

Ans. 4

Sol. The induced emf as given by Faraday's law of induction is

$$E = - B/v$$

$$l = 2R$$

= projection of ring perpendicular to the direction of v

$$= - B \times 2R \times v$$

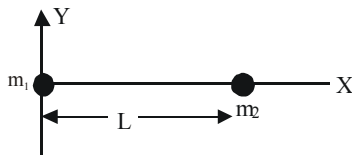
$$= - 2BvR.$$

18. The position of centre of mass of a system consisting of two particles of masses m_1 and m_2 separated by a distance L apart from m_1 is

- (1) $\frac{m_2 L}{m_1 + m_2}$ (2) $\frac{m_1 L}{m_1 + m_2}$
(3) $\frac{m_2 L}{m_1 - m_2}$ (4) $\frac{m_1 L}{m_1 - m_2}$

Ans. 1

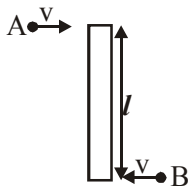
Sol. Let centre of first body be origin and line joining them is taken as x-axis



$$r_{cm} = \frac{m_1 r_1 + m_2 r_2}{m_1 + m_2} = \frac{m_1 \cdot 0 + m_2 L}{m_1 + m_2}$$

$$= \frac{m_2 L}{m_1 + m_2}$$

19. Two particles A and B of mass m each and moving with velocity v , hit the ends of a rigid bar of the same mass m and length l simultaneously and stick to the bar as shown in the figure. The bar is kept on a smooth horizontal plane. The linear and angular speed of the system (bar + particle) after the collision are



- (1) $v_{cm} = 0, \omega = \frac{12v}{7\ell}$ (2) $v_{cm} = 0, \omega = \frac{4v}{\ell}$
(3) $v_{cm} = 0, \omega = \frac{5v}{\ell}$ (4) $v_{cm} = 0, \omega = \frac{v}{5\ell}$

Ans : 1

Sol. From COLM,

$$mv - mv + 0 = 3m v_{cm}$$

$$\Rightarrow v_{cm} = 0$$

From COAM

$$2mv \times \frac{\ell}{2} = \left(\frac{m\ell^2}{12} + \frac{2m\ell^2}{4} \right) \omega$$

$$\Rightarrow \frac{12v}{7\ell}$$

20. A block slides down an inclined rough plane of inclination θ with constant velocity. It is then projected up the inclined plane with an initial speed u . How far up the incline will it move before coming to rest?

- (1) $u^2/4g \sin\theta$ (2) $u^2/g \sin\theta$
(3) $u^2/2g \sin\theta$ (4) u^2/g

Ans : 1

Sol. As acceleration is zero on the inclined plane this means $f = mg \sin\theta$

For upward motion net downward force is

$$f + mg \sin\theta = 2mg \sin\theta$$

$$\Rightarrow a = 2g \sin\theta$$

$$\Rightarrow \text{using } v^2 = u^2 + 2as$$

$$0 = u^2 - 4g \sin\theta s$$

$$\Rightarrow \frac{u^2}{4g \sin\theta} = s$$

21. Two particles X and Y having equal charges, after being accelerated through the same potential difference, enter a region of uniform magnetic field and describe circular paths of radii R_1 and R_2 , respectively. The ratio of the mass of X to that of Y is

- (1) $(R_1/R_2)^{1/2}$ (2) R_2/R_1
(3) $(R_1/R_2)^2$ (4) R_1/R_2

Ans. 3

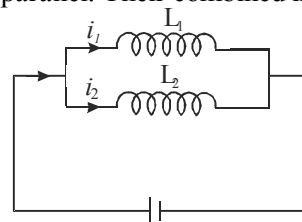
Sol. Let the masses be m_1 and m_2 respectively of X and Y. If E is energy gained by charged particle in electric field.

$$Bqv = \frac{mv^2}{r} \Rightarrow Bqr = \sqrt{2mE}$$

$$R_1 = \frac{\sqrt{2m_1 E}}{Bq}; R_2 = \frac{\sqrt{2m_2 E}}{Bq}$$

$$\frac{R_1}{R_2} = \sqrt{\frac{m_1}{m_2}} \Rightarrow \frac{m_1}{m_2} = \left(\frac{R_1}{R_2} \right)^2$$

22. Two inductances L_1 and L_2 are placed far apart and in parallel. Their combined inductance is



(1) $\frac{L_1 L_2}{L_1 + L_2}$ (2) $(L_1 + L_2)$

(3) $(L_1 + L_2) \frac{L_1}{L_2}$ (4) $(L_1 + L_2) \frac{L_2}{L_1}$

Ans. 1

Sol. $E = L_e \frac{di}{dt}$

$E = L_1 \frac{di_1}{dt} = L_2 \frac{di_2}{dt}$

$i = i_1 + i_2$

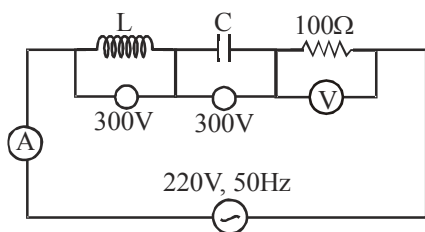
$\frac{di}{dt} = \frac{di_1}{dt} + \frac{di_2}{dt}$

$\frac{E}{L_e} = \frac{E}{L_1} + \frac{E}{L_2}$

$\frac{1}{L_e} = \frac{1}{L_1} + \frac{1}{L_2}$

$L_e = \frac{L_1 L_2}{L_1 + L_2}$

23. In the circuit shown in figure, what will be the readings of voltmeter and ammeter ?



- (1) 800 V, 2 A (2) 220 V, 2.2 A
(3) 300 V, 2 A (4) 100 V, 2 A.

Ans. 2

Sol. As $V_L = V_C = 300$ V,

and $V = \sqrt{V_R^2 + (V_L - V_C)^2}$

$\therefore V_R = V = 220$ V

Also $I = \frac{V}{R} = \frac{220}{100} = 2.2$ A

24. When a beam of light with wavelength, $\lambda = 6000 \text{ \AA}$, traveling in air, enters a glass medium whose refractive index is 1.5 then

- (1) Frequency of light remains constant
(2) Velocity of light increases by 1.5 times
(3) Frequency of light increases by 1.5 times
(4) Wavelength (λ) remains constant

Ans. 1

Sol. (i) When a beam of light enters from one medium to other, its frequency remains unchanged.

(ii) $V = n \lambda$ and $\mu = \frac{c}{v}$

$\therefore 1.5 = \frac{n \lambda_1}{n \lambda_2}$

or $1.5 = \frac{\lambda_1}{\lambda_2}$ or $\lambda_2 = \frac{\lambda_1}{1.5}$

Hence wavelength decreases by 1.5 times.

25. An artificial satellite moving in a circular orbit around the earth has a total (K.E. + P.E.) = E_0 . Its potential energy is

- (1) $-E_0$ (2) $1.5 E_0$
(3) $2 E_0$ (4) E_0 .

Ans. 3

Sol. Total energy = kinetic energy + Potential energy

$E_0 = \frac{1}{2} m v^2 - \frac{GMm}{r}$... (i)

Further, $\frac{m v^2}{r} = \frac{GMm}{r^2}$

or $\frac{1}{2} m v^2 = \frac{GMm}{2r}$... (ii)

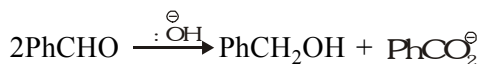
Substituting the value of $\frac{1}{2} m v^2$ in equation (i)

from equation (ii), we get

$E_0 = \frac{GMm}{2r} - \frac{GMm}{r} = -\frac{GMm}{2r}$

Therefore, P.E. = $-\frac{GMm}{r} = 2E_0$

26. In Cannizzaro reaction given below :-



the slowest step is :-

- (1) The abstraction of proton from the carboxylic group
(2) The deprotonation of PhCH_2OH
(3) The attack of $:\text{OH}^-$ at the carboxyl group
(4) The transfer of hydride to the carbonyl group

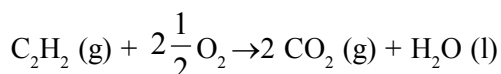
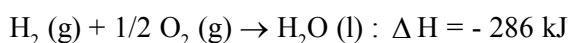
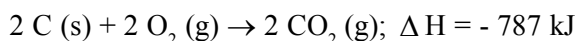
Ans . 4

27. Let the solubility of AgCl in water, in 0.01 M CaCl_2 , in 0.01 M NaCl and in 0.05 M AgNO_3 be s_1, s_2, s_3 and s_4 respectively. Which of the following relations between these quantities is correct

- (1) $s_1 > s_2 > s_3 > s_4$ (2) $s_1 > s_2 = s_3 > s_4$
(3) $s_4 > s_2 > s_3 > s_1$ (4) $s_1 > s_3 > s_2 > s_4$

Ans . 4

28. Given that



$$\Delta H = - 1301 \text{ kJ}$$

Heat of formation of acetylene is

- (1) -1802 kJ (2) $+1802 \text{ kJ}$
(3) -800 kJ (4) $+228 \text{ kJ}$

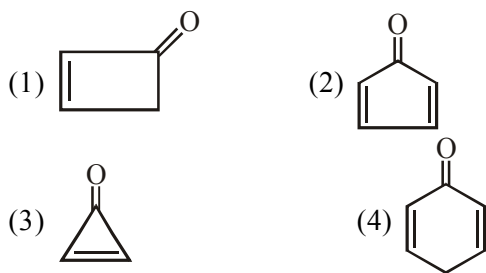
Ans . 4

29. Radioactivity of a sample ($z = 22$) decreases 90% after 10 years. What will be the half-life of the sample?

- (1) 5 years (2) 2 years
(3) 3 years (4) 10 years

Ans . 3

30. The most reactive compound towards $\text{CH}_3\text{-MgCl}$ is :



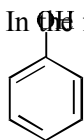
Ans . 2

31. 'a' and 'b' are van der Waals' constants for gases. Chlorine is more easily liquefied than ethane because

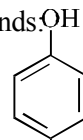
- (1) a for $\text{Cl}_2 > a$ for C_2H_6 but b for $\text{Cl}_2 < b$ for C_2H_6
(2) a for $\text{Cl}_2 < a$ for C_2H_6 but b for $\text{Cl}_2 > b$ for C_2H_6
(3) a and b for $\text{Cl}_2 > a$ and b for C_2H_6
(4) a and b for $\text{Cl}_2 < a$ and b for C_2H_6

Ans . 1

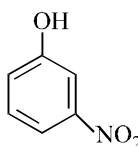
32. In the following compounds:



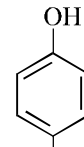
(I)



(II)



(III)



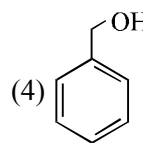
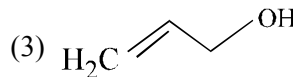
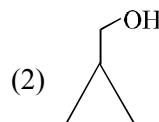
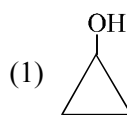
(IV)

The order of acidity is:

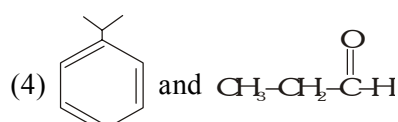
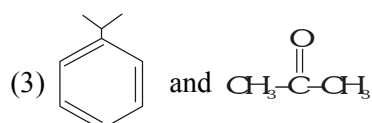
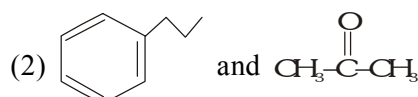
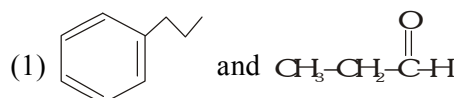
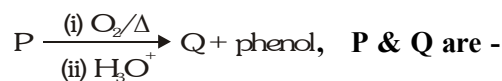
- (1) $\text{III} > \text{IV} > \text{I} > \text{II}$ (2) $\text{I} > \text{IV} > \text{III} > \text{II}$
(3) $\text{II} > \text{I} > \text{III} > \text{IV}$ (4) $\text{IV} > \text{III} > \text{I} > \text{II}$

Ans . 4

33. Which of the following alcohol shows fastest reaction with HI ?



Ans . 2



Ans . 3

35. Gold numbers of protective colloids A, B, C and D are 0.50, 0.01, 0.10 and 0.005, respectively. The correct order of their protective powers is

- (1) $D < A < C < B$ (2) $C < B < D < A$
(3) $A < C < B < D$ (4) $B < D < A < C$

Ans . 3

36. The reaction of $\text{CH}_3\text{OC}_2\text{H}_5$ with HI gives

- (1) CH_3I
(2) $\text{C}_2\text{H}_5\text{OH}$
(3) $\text{CH}_3\text{I} + \text{C}_2\text{H}_5\text{OH}$
(4) $\text{C}_2\text{H}_5\text{I} + \text{CH}_3\text{OH}$

Ans . 3

37. Anti-Markownikoff's addition of HBr is not observed in –

- (1) Propene
(2) But-2-ene
(3) Butene (4) Pent-2-ene

Ans . 2

38. The reaction quotient (Q) for the reaction $\text{N}_2(\text{g}) + 3\text{H}_2(\text{g}) \rightleftharpoons 2\text{NH}_3(\text{g})$

is given by $Q = \frac{[\text{NH}_3]^2}{[\text{N}_2][\text{H}_2]^3}$. The reaction will proceed from right to left if

- (1) $Q < K_c$ (2) $Q > K_c$
(3) $Q = 0$ (4) $Q = K_c$

Ans . 2

39. The oxidation state of Fe in the brown ring complex : $[\text{Fe}(\text{H}_2\text{O})_5\text{NO}] \text{SO}_4$ is :-

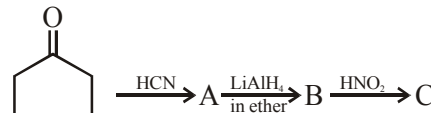
- (1) +2 (2) +1
(3) +3 (4) 0

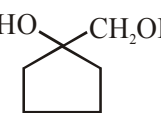
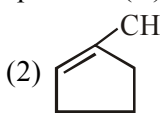
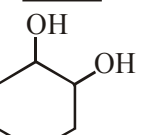
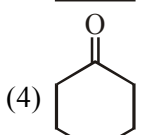
Ans . 2

40. When O_2 is converted into O_2^+ ;

- (1) Both paramagnetic character and bond order increase
(2) Bond order decreases
(3) Paramagnetic character increases
(4) Paramagnetic character decreases and the bond order increases

Ans . 4

41. 
In above reaction major product (C) is :

- (1)  (2) 
(3)  (4) 

Ans . 4

42. If a is the length of unit cell, then which one is correct relationship -

- (1) For simple cubic lattice, Radius of metal

$$\text{atom} = \frac{a}{2}$$

- (2) For bcc lattice, Radius of metal atom

$$= \frac{\sqrt{3}a}{4}$$

- (3) For fcc lattice, Radius of metal

$$\text{atom} = \frac{a}{2\sqrt{2}}$$

- (4) All of these

Ans . 4

43. The correct order of O-O bond length in O_2 , H_2O_2 and O_3 is

- (1) $\text{O}_2 > \text{O}_3 > \text{H}_2\text{O}_2$ (2) $\text{O}_3 > \text{H}_2\text{O}_2 > \text{O}_2$
(3) $\text{O}_2 > \text{H}_2\text{O} > \text{O}_3$ (4) $\text{H}_2\text{O}_2 > \text{O}_3 > \text{O}_2$

Ans . 4

44. According to Bohr's theory, the angular momentum of an electron in 5th orbit is

- (1) $25 \frac{h}{\pi}$ (2) $1.0 \frac{h}{\pi}$
(3) $10 \frac{h}{\pi}$ (4) $2.5 \frac{h}{\pi}$

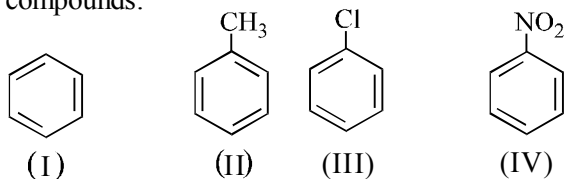
Ans . 4

45. In which of the following complex ion, the central metal ion is in a state of sp^3d^2 hybridisation ?

- (1) $[\text{CoF}_6]^{3-}$ (2) $[\text{Co}(\text{NH}_3)_6]^{3+}$
(3) $[\text{Fe}(\text{CN})_6]^{3-}$ (4) $[\text{Cr}(\text{NH}_3)_6]^{3+}$

Ans . 1

46. Identify the correct order of reactivity in electrophilic substitution reaction of the following compounds:



- (1) I > II > III > IV (2) IV > III > II > I
 (3) II > I > III > IV (4) II > III > I > IV

Ans . 3

47. The wavelength of the third line of the Balmer series for a hydrogen atom is :

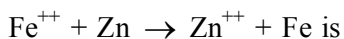
- (1) $\frac{21}{100R_H}$ (2) $\frac{100}{21R_H}$
 (3) $\frac{21R_H}{100}$ (4) $\frac{100R_H}{21}$

Ans . 2

48. The standard electrode potential for the half cell reactions are :



The E.M.F. of the cell reaction :



- (1) +1.20 V (2) +0.32 V
 (3) -0.32 V (4) -1.20 V

Ans . 2

49. Which one of the following statement is FALSE ?

- (1) Raoult's law states that the vapour pressure of a components over a solution is proportional to its mole fraction
 (2) The osmotic pressure (π) of a solution is given by the equation $\pi = MRT$, where M is the molarity of the solution
 (3) The correct order of osmotic pressure for 0.01 M aqueous solution of each compound is $\text{BaCl}_2 > \text{KCl} > \text{CH}_3\text{COOH} > \text{sucrose}$
 (4) Two sucrose solutions of same molality prepared in different solvents will have the same freezing point depression.

Ans . 4

50. Arrange Cl^- , Br^- , I^- in the order of decreasing reducing power –

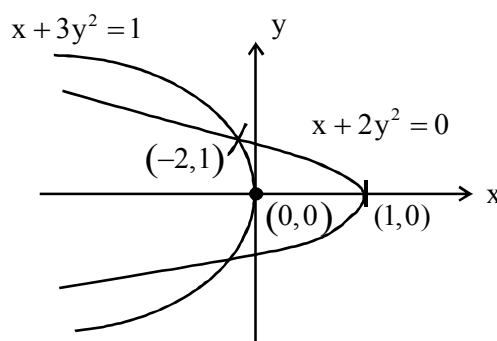
- (1) $\text{Cl}^- > \text{Br}^- > \text{I}^-$ (2) $\text{I}^- > \text{Br}^- > \text{Cl}^-$ (3)
 $\text{Br}^- > \text{Cl}^- > \text{I}^-$ (4) $\text{I}^- > \text{Cl}^- > \text{Br}^-$

Ans . 2

51. The area of the plane region bounded by the curve $x + 2y^2 = 0$ and $x + 3y^2 = 1$ is equal to

- (1) $\frac{4}{3}$ (2) $\frac{5}{3}$
 (3) $\frac{1}{3}$ (4) $\frac{2}{3}$

Ans. 1



Sol.

$$x + 3y^2 = 1$$

$$x + 2y^2 = 0$$

$$\text{Solving } y = \pm 1; x = -2$$

$$\text{Required area } \left| \int_{-1}^1 (x_1 - x_2) dy \right|$$

$$= \left| \int_{-1}^1 (1 - y^2) dy \right|$$

$$= \frac{4}{3} \text{ sq. units}$$

52. The general solutions of

$$y^2 dx + (x^2 - xy + y^2) dy = 0 \text{ is}$$

- (1) $\tan^{-1} \frac{x}{y} + \log_e |y| + c = 0$
 (2) $2 \tan^{-1} \frac{x}{y} + \ln |x| + c = 0$
 (3) $\ln |y| + \sqrt{x^2 + y^2} + \ln y + c = 0$
 (4) None of these

Ans. 1

Sol. $dx + \left(\frac{x^2 - xy + y^2}{y^2} \right) dy = 0$

$$\frac{dx}{dy} + \left(\frac{x}{y} \right)^2 - \left(\frac{x}{y} \right) + 1 = 0$$

$$\frac{x}{y} = v$$

$$\frac{dx}{dy} = v + y \frac{dv}{dy}$$

$$y \frac{dv}{dy} = -(v+1)$$

$$\Rightarrow \tan^{-1} v + \log|y| + c = 0$$

$$\Rightarrow \tan^{-1} \frac{x}{y} + \ln|y| + c = 0$$

53. The solutions of the differential equation

$$\frac{dy}{dx} + \frac{2x}{1+x^2} y = \frac{1}{(1+x^2)^2} \text{ is}$$

(1) $y(1-x^2) = \tan^{-1} x + c$

(2) $y(1+x^2) = \tan^{-1} x + c$

(3) $y(1+x^2)^2 = \tan^{-1} x + c$

(4) $y(1-x^2)^2 = \tan^{-1} x + c$

Ans. 2

Sol. $\frac{dy}{dx} + \frac{2x}{1+x^2} y = \frac{1}{(1+x^2)^2}$

$$P = \frac{2x}{1+x^2} \quad Q = \frac{1}{(1+x^2)^2}$$

$$I.F = e^{\int P dx} = 1+x^2$$

$$y(1+x^2) = \int (1+x^2) \frac{1}{(1+x^2)^2} dx + c$$

$$y(1+x^2) = \tan^{-1} x + c$$

54. If $\vec{a}, \vec{b}, \vec{c}$ are unit coplanar vectors, then

$$\begin{bmatrix} 2\vec{a} - \vec{b} & 2\vec{b} - \vec{c} & 2\vec{c} - \vec{a} \end{bmatrix} \text{ is equal to}$$

(1) 1 (2) 0 (3) $-\sqrt{3}$ (4) $\sqrt{3}$

Ans. 2

Sol. $\therefore 2\vec{a} - \vec{b}, 2\vec{b} - \vec{c}, 2\vec{c} - \vec{a}$
are also coplaner, thus

$$\begin{bmatrix} 2\vec{a} - \vec{b} & 2\vec{b} - \vec{c} & 2\vec{c} - \vec{a} \end{bmatrix} = 0$$

55. If $(\vec{a} \times \vec{b})^2 + (\vec{a} \cdot \vec{b})^2 = 676$ and $|\vec{b}| = 2$, then $|\vec{a}|$ is equal to

(1) 13

(2) 26

(3) 39

(4) None of these

Ans. 1

Sol. $(|\vec{a}| |\vec{b}| \sin \theta \hat{n})^2 + (|\vec{a}| |\vec{b}| \cos \theta)^2 = 676$

$$|\vec{a}|^2 |\vec{b}|^2 = 676$$

$$|\vec{a}| = 13$$

56. If $f(x) = \frac{e^x}{1+e^x}$

$$I_1 = \int_{f(-a)}^{f(a)} xg(x(1-x)) dx \text{ and}$$

$$I_2 = \int_{f(-a)}^{f(a)} g(x(1-x)) dx \text{ then the value of } I_2 : I_1 =$$

(1) 2

(2) -3

(3) -1

(4) 1

Ans. 1

Sol. $f(a) + f(-a) = \frac{e^a}{1+e^a} + \frac{1}{e^a+1} = 1$

$$\Rightarrow f(a) = 1 - f(-a)$$

Let $f(-a) = t$

$$\Rightarrow f(a) = 1 - t$$

$$I_1 = \int_t^{1-t} xg(x(1-x)) dx$$

$$I_1 = \int_t^{1-t} (1-x)g(x(1-x)) dx$$

$$2I_1 = \int_t^{1-t} g(x(1-x))(x+1-x) dx = I_2$$

$$\Rightarrow 2I_1 = I_2$$

$$\frac{I_2}{I_1} = 2$$

57. If $D_k = \begin{vmatrix} 1 & n & n \\ 2k & n^2 + n + 1 & n^2 + n \\ 2k - 1 & n^2 & n^2 + n + 1 \end{vmatrix}$ and

$\sum_{k=1}^n D_k = 56$ then n equals

- (1) 4 (2) 6
(3) 8 (4) None of these

Ans. 4

Sol: $\sum_{k=1}^n D_k = \begin{vmatrix} \sum_{k=1}^n 1 & n & n \\ 2\sum_{k=1}^n k & n^2 + n + 1 & n^2 + n \\ 2\sum_{k=1}^n k - \sum_{k=1}^n 1 & n^2 & n^2 + n + 1 \end{vmatrix}$

$\Rightarrow \begin{vmatrix} n & 0 & 0 \\ n^2 + n & 1 & 0 \\ n & 0 & n + 1 \end{vmatrix} = 56$

$\Rightarrow n(n+1) = 56$

$\Rightarrow n = 7$

58. The mirror image of the parabola $y^2 = 4x$ in the tangent to the parabola at the point (1,2) is

- (1) $(x-1)^2 = 4(y+1)$ (2) $(x+1)^2 = 4(y+1)$
(3) $(x+1)^2 = 4(y-1)$ (4) $(x-1)^2 = 4(y-1)$

Ans. 3

Sol. Any point on given parabola is $(t^2, 2t)$. The equation of tangent at (1,2) is $x - y + 1 = 0$ image of (h,k) of the point $(t^2, 2t)$ in $x - y + 1 = 0$

$\frac{h - t^2}{1} = \frac{k - 2t}{-1} = \frac{-2(t^2 - 2t + 1)}{1 + 1}$

$h = 2t - 1$

$k = t^2 + 1$

elimintary $(h+1)^2 = 4(k-1)$

59. The number of distinct values of a 2×2 determinant whose entries are from the set $\{-1, 0, 1\}$ is

- (1) 3 (2) 4 (3) 5 (4) 6

Ans. 3

Sol. Possible values are $-2, -1, 0, 1, 2$

$\begin{vmatrix} 1 & 0 \\ -1 & 1 \end{vmatrix} = 1$ $\begin{vmatrix} 1 & -1 \\ 0 & 0 \end{vmatrix} = 0$

$\begin{vmatrix} 0 & 1 \\ 1 & -1 \end{vmatrix} = -1$ $\begin{vmatrix} 1 & -1 \\ 1 & 1 \end{vmatrix} = 2$

$\begin{vmatrix} -1 & 1 \\ 1 & 1 \end{vmatrix} = -2$

60. The lines $\frac{x-2}{1} = \frac{y-3}{1} = \frac{z-4}{-k}$ and

$\frac{x-1}{k} = \frac{y-4}{2} = \frac{z-5}{1}$ are co-planar if

(where $k \neq -3$)

- (1) $k = 0$ (2) $k = 1$
(3) $k = 3$ (4) $k = 4$

Ans. 1

Sol. $\begin{vmatrix} -1 & 1 & 1 \\ 1 & 1 & -k \\ k & 2 & 1 \end{vmatrix} = 0$

$\Rightarrow -1(1+2k) - 1(1+k^2) + 1(2-k) = 0$

$\Rightarrow -k^2 - 3k^2 = 0$

$\Rightarrow k = 0$ or $k = -3$

61. If the sum to infinity of the series

$1 + 4x + 7x^2 + 10x^3 + \dots + \infty$ is $\frac{35}{16}$ then x equals

- (1) $\frac{1}{5}$ (2) $\frac{19}{7}$
(3) $\frac{4}{5}$ (4) $\frac{2}{3}$

Ans. 1

S o l

$$\begin{aligned} s_{\infty} &= 1 + 4x + 7x^2 + 10x^3 + \dots \infty \\ xs_{\infty} &= x + 4x^2 + 7x^3 + \dots \infty \\ \hline (1-x)s_{\infty} &= 1 + 3x + 3x^2 + 3x^3 + \dots \infty \end{aligned}$$

$\Rightarrow (1-x)\frac{35}{16} = 1 + \frac{3x}{1-x}$

$\Rightarrow 35x^2 - 102x + 19 = 0$

$\Rightarrow (7x-19)(5x-1) = 0$

$$\Rightarrow x = \frac{19}{7} \quad x = \frac{1}{5}$$

$$\therefore |x| < 1 \quad ; \quad x = \frac{1}{5}$$

62. If $a = \cos \frac{2\pi}{7} + i \sin \frac{2\pi}{7}$, then the quadratic equation

whose roots are $\alpha = a + a^2 + a^4$ and

$\beta = a^3 + a^5 + a^6$ is

(1) $x^2 - x + 2 = 0$ (2) $x^2 + x - 2 = 0$

(3) $x^2 - x - 2 = 0$ (4) $x^2 + x + 2 = 0$

Ans. 4

Sol. $a = \cos \frac{2\pi}{7} + i \sin \frac{2\pi}{7}$

$$a^7 = 1$$

$$s = \alpha + \beta = a + a^2 + a^4 + a^3 + a^5 + a^6$$

$$s = a \frac{(1 - a^6)}{1 - a} = -1$$

$$p = \alpha\beta = (a + a^2 + a^4)(a^3 + a^5 + a^6)$$

$$= a^4 + a^6 + 1 + a^5 + 1 + a + 1 + a^2 + a^3$$

$$= 3 - 1 = 2$$

$$\text{Reqd eqn} = x^2 - sx + p = 0$$

$$x^2 + x + 2 = 0$$

63. The point of the curve $y = x^2$ which is closest to

$(4, -\frac{1}{2})$ is

(1) (1, 1) (2) (2, 4)

(3) $(\frac{2}{3}, \frac{4}{9})$ (4) $(\frac{4}{3}, \frac{16}{9})$

Ans. 1

Sol. $L = \sqrt{(x-4)^2 + (y + \frac{1}{2})^2}$

$$L = (x-4)^2 + (y + \frac{1}{2})^2$$

$$L' = x^4 + 2x^2 - 8x$$

$$L' = 4x^3 + 4x - 8 = 0$$

$$\Rightarrow x = 1$$

$$L'' = 12x^2 + 4$$

$$L'' = 16 > 0$$

So D is minimum at $x = 1$ i.e at (1, 1)

64. The value of $\int \frac{(x+1)}{x(1+xe^x)^2} dx$ is

(1) $\frac{1}{1+xe^x} + c$ (2) $\ln \left| \frac{x+e^x}{1+xe^x} \right| + c$

(3) $\ln \left| \frac{x+1}{1+xe^x} \right| + c$ (4) None of these

Ans. 4

Sol. Let $1 + xe^x = t$

$$(x+1)e^x dx = dt$$

$$I = \int \frac{dt}{(t-1)t^2} = \int -\frac{1}{t^2} - \frac{1}{t} + \frac{1}{t-1} dt$$

$$= \frac{1}{t} - \log|t| + \log|t-1| + C$$

$$= \frac{1}{1+xe^x} + \log \left| \frac{xe^x}{1+xe^x} \right| + C$$

65. If $f(x) = \min\{x+2, 1, 2-x\}$, then $\int_{-2}^2 f(x) dx$

equals

(1) 1 (2) 2

(3) 3 (4) 0

Ans. 3

Sol. $\int_{-2}^{-1} (x+2) dx + \int_{-1}^1 dx + \int_1^2 (2-x) dx$

$$= \frac{1}{2} + 2 + \frac{1}{2} = 3$$

66. If $\cos \alpha + \cos \beta + \cos \gamma = \sin \alpha + \sin \beta + \sin \gamma = 0$

then $\cos 3\alpha + \cos 3\beta + \cos 3\gamma =$

(1) 0 (2) $\cos(\alpha + \beta + \gamma)$

(3) $3 \cos(\alpha + \beta + \gamma)$ (4) $3 \sin(\alpha + \beta + \gamma)$

Ans. 3

Sol. $\cos \alpha + \cos \beta + \cos \gamma = 0$

$$\sin \alpha + \sin \beta + \sin \gamma = 0$$

$$\text{let } a = \cos \alpha + i \sin \alpha$$

$$b = \cos \beta + i \sin \beta$$

$$c = \cos \gamma + i \sin \gamma$$

$$\therefore a + b + c = 0$$

$$a^3 + b^3 + c^3 - 3abc = 0$$

$$\Rightarrow (\cos 3\alpha + i \sin 3\alpha)(\cos 3\beta + i \sin 3\beta) + (\cos 3\gamma + i \sin 3\gamma)$$

$$= 3[\cos(\alpha + \beta + \gamma) + i \sin(\alpha + \beta + \gamma)]$$

$$\Rightarrow \cos 3\alpha + \cos 3\beta + \cos 3\gamma = 3 \cos(\alpha + \beta + \gamma)$$

67. The value of $\int \frac{(x^2 - 1)dx}{x^3 \sqrt{2x^4 - 2x^2 + 1}}$ is

(1) $2\sqrt{2 - \frac{2}{x^2} + \frac{1}{x^4}} + C$

(2) $2\sqrt{2 + \frac{2}{x^2} + \frac{1}{x^4}} + C$

(3) $\frac{1}{2}\sqrt{2 - \frac{2}{x^2} + \frac{1}{x^4}} + C$

(4) None of these

Ans. 3

Sol. $I = \int \frac{\left(\frac{1}{x^3} - \frac{1}{x^5}\right)dx}{\sqrt{2 - \frac{2}{x^2} + \frac{1}{x^4}}}$

$$2 - \frac{2}{x^2} + \frac{1}{x^4} = t$$

$$\left(\frac{4}{x^3} - \frac{4}{x^5}\right)dx = dt$$

$$I = \frac{1}{4} \int \frac{dt}{\sqrt{t}} = \frac{1}{2} \sqrt{2 - \frac{2}{x^2} + \frac{1}{x^4}} + C$$

68. N be the set of natural numbers. The relation R defined on $N \times N$ as follows

$$(a, b) R (c, d) \Leftrightarrow a + d = b + c \text{ is}$$

(1) Not reflexive (2) Not symmetric

(3) Transitive (4) None of these

Ans. 3

Sol. 1. $(a, b) R (a, b) \Leftrightarrow a + b = b + a$ is

$$\therefore R \text{ is reflexive}$$

2. $(a, b) R (c, d)$

$$\Rightarrow a + d = b + c$$

$$= c + b = d + a$$

$$= (c, d) R (a, b)$$

3. $(a, b) R (c, d) \& (c, d) R (e, f)$

$$\Rightarrow (a + d) = (b + c) \& c + f = d + e$$

$$\Rightarrow a + d + c + f = b + c + d + e$$

$$\Rightarrow a + f = b + e$$

$$\Rightarrow (a, b) R (e, f)$$

$$\therefore R \text{ is transitive}$$

69. Co-ordinates of a point on the curve $y = x \log x$ at which the normal is parallel to the line

$$2x - 2y = 3 \text{ are}$$

(1) $(0, 0)$

(2) (e, e)

(3) $(e^2, 2e^2)$

(4) $(e^2, -2e^2)$

Ans. 4

Sol. Given $y = x \ln x$

$$\frac{dy}{dx} = 1 + \ln x$$

$$\text{Slope of normal} = \frac{-1}{1 + \ln x}$$

$$\text{So } \frac{-1}{1 + \ln x} = 1 \Rightarrow x = e^{-2}$$

$$\Rightarrow y = -2e^{-2}$$

So co-ordinate of pt in $(e^{-2}, -2e^{-2})$

70. If $f''(x) = -f(x)$ where $f(x)$ is a continuous double differentiable function and $g(x) = f'(x)$. If

$$F(x) = \left(f\left(\frac{x}{2}\right)\right)^2 + \left(g\left(\frac{x}{2}\right)\right)^2 \text{ and } F(5) = 5, \text{ then}$$

$$F(10) =$$

(1) 0

(2) 5

(3) 10

(4) 25

Ans. 2

Sol. $f''(x) = -f(x)$

$$\Rightarrow g'(x) = -f(x)$$

$$\text{Also } F(x) = \left(f\left(\frac{x}{2}\right)\right)^2 + \left(g\left(\frac{x}{2}\right)\right)^2$$

$$F'(x) = 2f\left(\frac{x}{2}\right) \times f'\left(\frac{x}{2}\right) \times \frac{1}{2} + 2g\left(\frac{x}{2}\right) \times g'\left(\frac{x}{2}\right) \times \frac{1}{2}$$

$$F'(x) = 0 \Rightarrow F(x) = C$$

$$F(5) = 5$$

71. The number of real solution(s) of the equation

$$7\sqrt{x} + 8\sqrt{-x} + \frac{15}{x^3} = 98 \text{ is/are}$$

- (1) 0 (2) 1
(3) 2 (4) Infinite

Ans. 1

Sol. $\sqrt{x}; x \geq 0$ $\sqrt{-x} -x \geq 0$
 $x \leq 0$

But $x = 0$ is also not possible

$\therefore \frac{15}{x^3}$ is undefined

72. If the eccentricity of the two ellipse

$$\frac{x^2}{169} + \frac{y^2}{25} = 1 \text{ and } \frac{x^2}{a^2} + \frac{y^2}{b^2} = 1 \text{ are equal, then the}$$

value of $\frac{a}{b} =$

- (1) $\frac{5}{13}$ (2) $\frac{6}{13}$
(3) $\frac{13}{5}$ (4) $\frac{13}{6}$

Ans. 3

Sol. $\frac{x^2}{169} + \frac{y^2}{5^2} = 1$

$$e = \frac{12}{3}; e' = \sqrt{1 - \frac{b^2}{a^2}}$$

$$\Rightarrow \frac{b}{a} = \frac{5}{13} \Rightarrow \frac{a}{b} = \frac{13}{5}$$

73. $\lim_{x \rightarrow 0} (\operatorname{cosec} x)^{\frac{1}{\log_e x}}$ is equal to

- (1) 0 (2) 1
(3) $1/e$ (4) None of these

Ans. 3

Sol. $\ln y = \lim_{x \rightarrow 0} \frac{\ln \operatorname{cosec} x}{\ln x}$

$$= \lim_{x \rightarrow 0} \frac{-\cot x}{1/x} = -1$$

$$y = e^{-1}$$

74. Let $f(x) = \begin{cases} x^p \sin \frac{1}{x} & ; x \neq 0 \\ 0 & ; x = 0 \end{cases}$, then $f(x)$ is

continuous but not differentiable at $x = 0$ if

- (1) $0 < p \leq 1$ (2) $1 \leq p < \infty$
(3) $-\infty < p \leq 0$ (4) $p = 0$

Ans. 1

Sol. $\lim_{x \rightarrow 0} x^p \sin \frac{1}{x} = 0; 0 < p < \infty$

$$\text{RHD} = \lim_{h \rightarrow 0} \frac{h^p \sin \frac{1}{h} - 0}{h}$$

$$\text{LED} = \lim_{h \rightarrow 0} \frac{(-h^p) \sin \left(-\frac{1}{h} \right) - 0}{-h}$$

$\therefore f$ is not differentiable at $x > 0$

$\therefore p \leq 1$

So $p \in (0, 1]$

75. If $A = 1000^{1000}$; $B = 1001^{999}$, then

- (1) $A > B$ (2) $A = B$
(3) $A < B$ (4) None of these

Ans. 1

Sol. Since, $\left(1 + \frac{1}{n}\right)^n < 3 \quad \forall n \in \mathbb{N}$

$$\text{Now, } \frac{(1001)^{999}}{(1000)^{1000}} = \frac{1}{1001} \left(\frac{1001}{1000} \right)^{1000}$$

$$= \frac{1}{1001} \left(1 + \frac{1}{1000} \right)^{1000}$$

$$< \frac{1}{1001} \cdot 3 < 1$$

$$\Rightarrow 1001^{999} < 1000^{1000}$$

$B < A$

76. The maximum value of $f(x) = \frac{x}{4+x+x^2}$ on $[-1, 1]$ is

- (1) $\frac{-1}{4}$ (2) $\frac{-1}{3}$ (3) $\frac{1}{6}$ (4) $\frac{1}{5}$

Ans. 3

Sol. $f'(x) = \frac{4-x^2}{(4+x+x^2)} = 0 \Rightarrow x = \pm 2$

Both values are not in $[-1, 1]$ so

$f(-1) = \frac{-1}{4}$ $f(1) = \frac{1}{6}$ maximum

77. Let $f : \mathbb{R} \rightarrow \mathbb{R}$ be a differentiable function having

$f(2) = 6, f'(2) = \frac{1}{48}$ then, $\lim_{x \rightarrow 2} \int_6^{f(x)} \frac{4t^3}{x-2} dt =$

- (1) 18 (2) 12
(3) 24 (4) 36

Ans. 1

Sol. $\lim_{x \rightarrow 2} \int_6^{f(x)} \frac{4t^3}{x-2} dt$

$= 4(f(x))^3 \times f'(x) = 4 \times 6^3 \times \frac{1}{48} = 18$

78. The number of common tangents to the circles

$x^2 + y^2 - 2x - 4y + 1 = 0$ and

$x^2 + y^2 - 12x - 16y + 91 = 0$ is

- (1) 1 (2) 2
(3) 3 (4) 4

Ans. 4

Sol. $C_1 = (1, 2) r_1 = 2$

$C_2 = (6, 8) r_2 = 3$

$C_1 C_2 = \sqrt{61} \quad r_1 + r_2 = 5$

So $C_1 C_2 > r_1 + r_2$

79. Two perpendicular tangents to the circle $x^2 + y^2 = a^2$ meet at P. Then, the locus of P has the equation

- (1) $x^2 + y^2 = 2a^2$ (2) $x^2 + y^2 = 3a^2$
(3) $x^2 + y^2 = 4a^2$ (4) None of these

Ans. 1

Sol. Director circle's equation

$x^2 + y^2 = 2a^2$

80. If the tangents at P and Q on the parabola meet in T, then SP, ST and SQ are in

- (1) AP (2) GP
(3) HP (4) None of these

Ans. 2

Sol. Since, tangent at P & Q on the parabola meet in T

$P(at_1^2, 2at_1), Q(at_2^2, 2at_2)$

$T = (at_1 t_2, a(t_1 + t_2))$

$SP = a(1 + t_1^2)$

$SQ = a(1 + t_2^2)$

$ST^2 = a^2(1 - t_1 t_2)^2 + a^2(t_1 + t_2)^2$

$= a(1 + t_2^2) \times a(1 + t_1^2) = SP \cdot SQ$

\therefore SP, ST, SQ are in G.P

81. Cattle and goats do not eat *Calotropis* because

- (1) It is tasteful to its predator
(2) It produces highly poisonous glycosides
(3) It possesses thorns
(4) It is hard to chew.

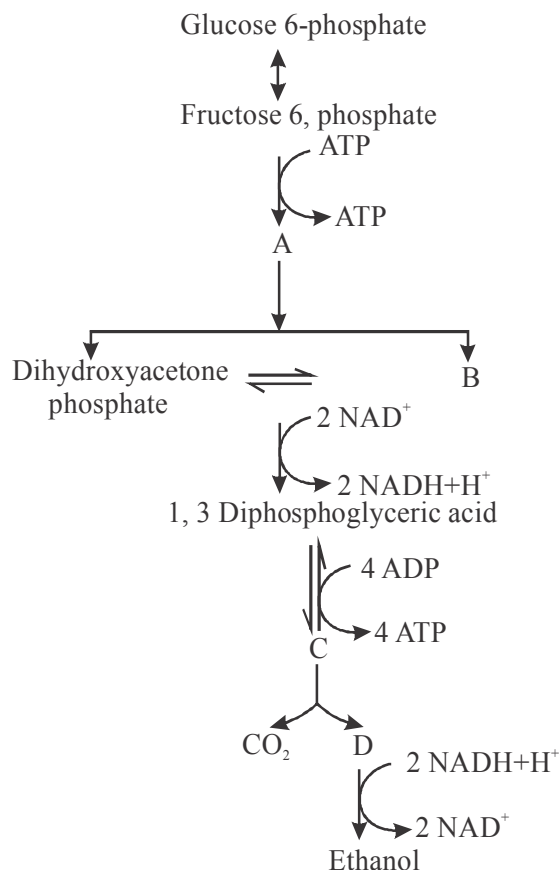
Ans : 2

82. In Mendelian dihybrid cross, when heterozygous round / yellow are self crossed, round / green offsprings are represented by the genotype

- (1) RrYy, RrYY, RRYy (2) Rryy, RRyy, rryy
(3) rrYy, RrYY (4) Rryy, RRyy

Ans : 4

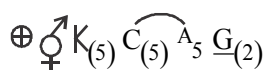
83. Observe the given flow chart showing steps of anaerobic respiration and identify the compounds A, B, C and D.



A	B	C	D
(1) Citrate	Pyruvic acid	Succinate	Glyceraldehyde 3-phosphate
(2) Succinate	Citrate	Pyruvic acid	Acetaldehyde
(3) Fructose 1,6-Bisphosphate	Glyceraldehyde 3-phosphate	Pyruvic acid	Acetaldehyde
(4) Glyceraldehyde 3-phosphate	Fructose 1,6-bisphosphate	Citric acid	Oxaloacetate

Ans : 3

84. The flower showing floral formula belongs to Family



- (1) Liliaceae (2) Solanaceae
(3) Poaceae (4) Ranunculaceae.

Ans : 2

85. The stalk which joins ovule to placenta is called

- (1) Hilum (2) Funicle
(3) Micropyle (4) Chalaza

Ans : 2

86. Verhulst-Pearl logistic growth is described by the equation

(1) $dN/dt = rN \left(\frac{K - N}{N} \right)$

(2) $dN/dt = rN \left(\frac{N - K}{N} \right)$

(3) $dN/dt = rN \left(\frac{K - N}{K} \right)$

(4) $dN/dt = rN \left(\frac{N - K}{K} \right)$

Ans : 3

87. The elements essential for the translocation of organic substances in the phloem are

- (1) Manganese and copper
(2) Boron and potassium
(3) Molybdenum and zinc
(4) Sulphur and potassium

Ans : 2

88. The coding strand of DNA has the following sequence:

5' - ACGTAC - 3'

What will be the sequence of mRNA?

- (1) UGCAUG (2) ACGUAC
(3) ACGTAC (4) TGCAUG

Ans : 2

89. Endosperm is formed during the double fertilisation by the fusion of

- (1) Two polar nuclei and one male gamete
(2) One polar nucleus and one male gamete
(3) Ovum and male gamete
(4) Two polar nuclei and two male gametes

Ans : 1

90. Which of the following plants is not pollinated by water?

- (1) *Vallisneria* (2) Water lily
(3) *Hydrilla* (4) *Zostera*

Ans : 2

91. In a pond, *Daphnia* is preyed upon by Prawn. Here, prawn and *Daphnia* are respectively

- (1) Tertiary consumer and secondary consumer
(2) Primary consumer and primary producer
(3) Secondary consumer and primary consumer
(4) Primary consumer and secondary consumer.

Ans : 3

92. Identify the correct from given statements.

- (I) Dicot leaves are dorsiventral whereas monocot leaves are isobilateral.
(II) Cellular slime moulds have multinucleate protoplasmic body called Plasmodium.
(III) During nitrification, ammonium ions are oxidised to nitrites with the help of nitrobacter and nitrites are changed to nitrates by Nitrosomonas bacteria.
(IV) The substrate for photorespiration are glucose and organic acids.
(V) Pepsin and renin enzymes are absent in invertebrates.

- (1) (I), (III) and (II)
(2) (I) only
(3) (III) and (IV) only
(4) (I), (III) and (IV) only

Ans : 2

93. An gymnosperm plant has 24 chromosomes in 'microspore mother cell'. The number of chromosomes in its endosperm will be
 (1) 12 (2) 36
 (3) 24 (4) 48

Ans : 1

94. The reserve food in euglenoids and diatoms respectively is
 (1) Cyanophycean starch, chitin
 (2) Paramylon, leucosin
 (3) Lipid globules, volutin globules
 (4) Leucosin, glycogen

Ans : 2

95. Match the column I with column II and III and select the correct option.

Column I	Column II	Column III
(P) Auxin	(i) Zeatin	(A) Barley Endosperm assay
(Q) Gibberellin	(ii) Dormin	(B) Avena curvature assay
(R) Cytokinin	(iii) Tryptophan	(C) Stomatal closure
(S) Abscisic acid	(iv) Mevalonic acid	(D) Tobacco pith culture

- (1) P-(iii)-B, Q-(iv)-A, R-(i)-D, S-(ii)-C
 (2) P-(iv)-C, Q-(ii)-B, R-(iii)-A, S-(i)-D
 (3) P-(i)-A, Q-(ii)-D, R-(iv)-C, S-(iii)-B
 (4) P-(ii)-D, Q-(iv)-A, R-(iii)-C, S-(i)-B

Ans : 1

96. The steps in DNA fingerprinting are given below. arrange them in the correct sequence
 (i) Transfer of separated DNA fragments to nitrocellulose membrane
 (ii) Isolation of DNA
 (iii) Hybridisation using labelled VNTR probe
 (iv) Separation of DNA fragments by electrophoresis
 (v) Detection of hybridised DNA fragments by autoradiography
 (vi) Digestion of DNA by restriction endonucleases
 (1) (i),(iii),(ii),(v),(vi),(iv)
 (2) (ii),(vi),(iv),(i),(iii),(v)
 (3) (iii),(ii),(v),(i),(iv),(vi)
 (4) (iv). (iii). (ii). (v). (i). (vi)

Ans : 2

97. Initiation codon of protein synthesis (in eukaryotes) is
 (1) GUA (2) GCA
 (3) CCA (4) AUG.

Ans : 4

98. Which of the following is not used in catalytic converters?
 (1) Rhodium (2) Palladium
 (3) Lead (4) Platinum

Ans : 3

99. The relative contribution of CH₄, CFCs and N₂O to total global warming is respectively
 (1) 6%, 14% and 20% (2) 25%, 6% and 10%
 (3) 30%, 24% and 2% (4) 20%, 14% and 6%.

Ans : 4

100. In a grassland ecosystem, the largest population in a pyramid of number is that of
 (1) Producers
 (2) Primary consumers
 (3) Secondary consumers
 (4) Tertiary consumers

Ans : 1

101. Find the incorrect statements
 (a) Drones (male honey bees) have grandfathers but no fathers.
 (b) Maximum life span is species characteristics
 (c) In parthenogenesis genetic variations are absent
 (d) Menstrual cycle is absent in Gorilla
 (e) Oviparity always need water medium for fertilization
 (f) Life span has absolutely no relation with the size of an organism.
 (1) a, b, c & d (2) c, d & e
 (3) a, e & f (4) b, c & e

Ans. 2

102. For the birth of 100 babies minimum how many meiotic divisions required ?
 (1) 100 (2) 125
 (3) 200 (4) 250

Ans. 2

103. What will be the day of ovulation of the duration of reproductive cycle in female is 20 days?
 (1) 10th day (2) 6th day
 (3) 14th day (4) 20th day

Ans. 2

104. What is the similarity between Darwin & Mendel?

- (1) Both believed in genes controlling a character
- (2) Both believed in transmission of characters from parents to offspring
- (3) Both worked on natural selection
- (4) Both believed on continuous variation.

Ans. 2

105. How Lamarck would explain the reason for increased antibiotic resistance in bacteria - "the experiment conducted by Lederberg"?

- (1) The antibiotic resistance property was present in bacteria from beginning. They got selected by nature when antibiotic was applied to the culture medium.
- (2) Few bacteria develop antibiotic resistance when antibiotic was applied and would survive.
- (3) Application of antibiotic in medium caused sudden change in the genetic system of bacteria, thus they developed antibiotic resistance.
- (4) Application of antibiotic would create a new species of bacteria that continued to live while pre-existing bacteria perished from culture plate.

Ans. 2

106. Haversian systems are found in the bones of

- (1) Scoliodon
- (2) Scoliodon and Psittacula
- (3) Rabbit and man
- (4) Panther, Python and Man

Ans. 3

107. Amniocentesis helps in

- (1) Determination of genetic disorder
- (2) Determination of sex of foetus
- (3) Determination of metabolic disorder
- (4) All of these

Ans. 4

108. IVF technique includes

- (1) GIFT
- (2) AI
- (3) IUT
- (4) All of these

Ans. 3

109. Which of the following is not a part of human evolution?

- (1) Bipedal locomotion
- (2) Loss of tail
- (3) Reduction of jaw bone
- (4) All are the parts of human evolution

Ans. 2

110. Which of the following diseases never affect genital/reproductive structures?

- (1) Mumps
- (2) AIDS
- (3) Gonorrhoea
- (4) Syphilis

Ans. 2

111. Which of the following conditions leads to infertility or sterility exclusively in male?

- (a) Klinefelter syndrome
 - (b) Down's syndrome
 - (c) Turner's syndrome
 - (d) Haemophilia
- (1) a
 - (2) a, b
 - (3) a, b & c
 - (4) a, b, c & d

Ans. 1

112. The confirmatory test for HIV before appearance of symptoms of AIDS

- (1) ELISA
- (2) Western blot
- (3) PCR
- (4) Both 2 & 3

Ans. 3

113. Which of the following is an example of artificial passive immunity?

- (1) Administration of Anti Tetanus Serum (ATS) after injury
- (2) Administration of polio vaccine
- (3) Transmission of antibodies via placenta from mother to foetus
- (4) Administration of antibodies to infant via breast feeding.

Ans. 1

114. Which of the following blood vessels contains the highest amount of urea?

- (1) Hepatic portal vein
- (2) Hepatic vein
- (3) Renal vein
- (4) Renal artery

Ans. 2

115. What would be the consequence if the SA node fails to initiate an impulse?

- (1) Ventricles stop contracting
- (2) Ventricles continue contraction at a slower rate.
- (3) Heart rate would be normal
- (4) Immediate cardiac arrest leading to death.

Ans. 2

116. How many of the following characters are present in animals?

- (a) Bilateral Symmetry
- (b) Cellular grade of organization
- (c) Binary fission
- (d) Amoeboid movement
- (e) Anaerobic respiration
- (f) Metagenesis

- (1) 2
- (2) 4
- (3) 5
- (4) 6

Ans. 4

117. Find the incorrect statements

- (a) Mother's milk is rich in iron and IgA.
- (b) Foetal ejection reflex results in release of oxytocin from foetal pituitary.
- (c) Major contributor of seminal plasma is seminal vesicle
- (d) Primary oocyte & WBC contain same number of chromosomes.
- (e) Removal of ovaries during 5th month of pregnancy may lead to abortion

- (1) a, b & e (2) b & d
- (3) b, d & e (4) a, b & c

Ans. 1

118. Which of the following dental formula, represent(s) human milk set ?

(a) $\frac{2123}{2123}$ (b) $\frac{2102}{2102}$

(c) $\frac{212}{212}$ (d) $\frac{0012}{0012}$

- (1) a (2) b
- (3) b & c (4) a & d

Ans. 3

119. Which of the followings are not the components of DNA?

- (a) Uracil
 - (b) Thiamine B₁
 - (c) Pentose sugar
 - (d) Double hydrogen bonds
 - (e) Glycosidic bonds
- (1) a (2) a & b
 - (3) a, d & e (4) a, c & e

Ans. 2

120. How many of the following structures are found in female cockroach only?

- (a) Spermatheca (b) Anal style
 - (c) Anal cerci (d) Common oviduct
- (1) 0 (2) 1
 - (3) 2 (4) 3

Ans. 3